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# Study of the properties of *Ru*-isotopes using the protonneutron interacting boson model (IBM-2)

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## Abstract:

The proton-neutron interacting boson model (IBM-2) has been used to make a schematic study of the Ruthenium (Ru) isotopes of mass region around A = 100 with Z = 44, and  $54 \le N \le 64$ . For each isotope of Ru the values of the IBM-2 Hamiltonian parameters, which yield an acceptable results for excitation energies in comparison with those of experimental data, have been determined. Fixed values of the effective charges ( $e_{\pi} = e_{\nu} = 0.102 \ e.b.$ ) and of the proton and neutron g factors ( $g_{\pi} = 1.0 \ \mu_N$  and  $g_{\nu} = 0.42 \ \mu_N$ ) have been chosen for all isotopes under study. The calculated electric B(E2) transitions, the magnetic dipole moments  $\mu_{2_1^+}$ , quadrupole moments of  $2_1^+$  state, B(M1) transitions and  $\delta(E2/M1)$  mixing ratios are in reasonable agreement with the experimental data.

#### Key word: Nuclear Structure Interacting Boson Model, Investigation of the Ru-isotpes Energies, B(E2) transition rates, and other properties. Model parameters as aSmooth function of neutron number

#### 1. Introduction

One of the main objectives of the study of nuclear physics is to understand the structure of nuclei. One of the interesting features of the IBM-2 is the prediction of a large class of states which are non-symmetric under the interchange of neutron bosons and proton bosons, and which are outside the model of the IBM-1. The lowest six excited  $2^+$  levels of the  $^{122-130}Te$ have been investigated nuclei experimently [1]. These levels have been identified and their decay properties have been characterized from gamma-ray excitation functions. In addition, the lifetime of these levels have been deduced using the dopplershift attenuation method Electromagnetic transition rates and E2/M1 multipole mixing ratios from the  $2_{2-6} \rightarrow 2_1$  transitions have been examind to identify the lowest mixedsymmetry states in these nuclei. The summed M1 stregth from the

 $2_{2-6} \rightarrow 2_1$  level agree rather well with neutron-proton interacting boson model predictions in the U(5) or O(6)limits for these Te nuclei. The energy spectra of the  $({}^{121-127}Xe, {}^{121-127}I)$  are cosidered in the (IBFM-2). Electromagnetic transition probabilities and branching ratio in odd 121-127 I isotopes have been investigated in [2]. Genilloud et al.[3] measured lifetime of excited states in 100 Ru. The absolute transition rates were extracted for these states

Parallel with these theoretical developments, several experiments were carried out to test the propreties of the low lying collective states in some nuclei of the IBM-2 [4-9]. The experimental work of Ref [10] was

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made to measure the absolute M1 and E2 transition strength in <sup>94</sup>Mo nucleus. The determination of branching ratios and E2/M1 mixing ratios in this nucleus was also made. Besides an identification of some mixed symmetry states was a chieved. These experimental result were in reasonable agreement with the

calculations of IBM-2. The emphasis in this work is on describing overall trends with constant parameters, rather than obtaining the best possible fit to the experimental data for each nucleus. This is done in an effort to find a set of IBM-2 Hamiltonian parameters which is appropriate for the entire isotopic chain.In the presesnt work, the calculations have been performed for the transitional nuclei  $[U(5) \rightarrow O(6)]$ of Ru-isotopes (with Z = 44 and  $54 \le N \le 64$ ) and devoted to study (i) the energy spectra and consequently the excitation energy of the lowest symmetric and mixed symmetric states (ii) the electric properties such as the quadrupole moment of the first excited state  $2_1^+$  and the E2 transition rates (iii) the magnetic properties which include the magnetic dipole moment of the first excited state  $2_1^+$ , the M1 transition strengths and the mixing ratios.

# 2. The interacting proton-neutron model

The proton- neutron interacting boson model, which is known as IBM-2, can make an explicit distinction between proton-and neutron -bosons. The Hamiltonian operator in the IBM-2 has the form

$$\hat{H} = \hat{H}_{\pi} + \hat{H}_{\nu} + \hat{V}_{\pi\nu}$$

where the first and second terms are describing the proton and neutron bosons while the third term is for describing the proton-neutron interaction. A simple schematic hamiltonian guided by microscopic consideration is given by [11]

$$\hat{H} = \not= \left(\hat{d}^{\dagger} \times \hat{\vec{d}}\right)_{\pi} + \not\in_{v} \left(\hat{d}^{\dagger} \times \hat{\vec{d}}\right)_{v} + \hat{V}_{\pi\pi} + \hat{V}_{vv} + \hat{K}\hat{Q}_{\pi}\hat{Q}_{v} + M_{\pi\sigma}$$
(2)

where  $\in_{\pi}$  and  $\in_{\nu}$  are the excitation energies for proton and neutron d-bosons respectively,  $\left(\hat{d}^{+} \times \hat{d}\right)_{\pi}$ and  $\left(d^{+} \times \hat{d}\right)_{\nu}$  are the d-boson number operators for protons and neutrons respectively, K is the strength of the quadrupole-quadrupole interaction between proton and neutron bosons,  $Q_{\pi}$  and  $Q_{\nu}$  are the quadrupole operators for proton and neutron bosons, respectively. Here  $Q_{\rho}$  ( $\rho = \pi$ or  $\nu$ ) is given by

$$\hat{Q}_{\rho} = \left(\hat{d}^{+} \times \hat{\tilde{s}}^{+} + \hat{s}^{+} \times \hat{\tilde{d}}^{(2)}\right)_{\rho}^{(2)} + \chi_{\rho} \left(\hat{d}^{+} \times \hat{\tilde{d}}^{+}\right)_{\rho}^{2},$$
(3)

where  $s^+, \tilde{s}, d^+$  and  $\tilde{d}$  are operators which create and annihilate *s* and *d* bosons respectively and  $\chi_{\rho}$  is the structure parameter. The residual twobody interaction between the like bosons is

$$V_{\rho\rho} = \sum_{L=0,2,4} \frac{1}{2} (2L+1)^{\frac{1}{2}} C_{L}^{\rho} \times \left[ (\hat{d}_{\rho}^{+} \times \hat{d}_{\rho}^{+})^{(L)} (\hat{d}_{\rho}^{-} \times \hat{d}_{\rho}^{-})^{(L)} \right]^{(0)}$$
(4)

The  $C_L^{\rho}$  parameter is well known to effect only minor details of the energy spectrum. Finally  $M_{\pi\nu}$  is the so-called Majorana operator and given by [13]

$$M_{\pi\nu} = \xi_2 \Big[ \hat{s}_{\nu}^+ \times \hat{d}_{\pi}^+ - \hat{s}_{\pi}^+ \times \hat{d}_{\nu}^+ \Big]^{(2)} \Big[ \hat{s}_{\nu}^- \times \hat{d}_{\pi}^- - \hat{s}_{\pi}^- \times \hat{d}_{\nu}^- \Big]^{(2)}$$

$$-2\sum_{k=l,3}\xi_{k}\left[\hat{d}_{\nu}^{+}\times\hat{d}_{\pi}^{+}\right]^{(k)}\left[\hat{\widetilde{d}}_{\nu}\times\hat{\widetilde{d}}_{\pi}^{-}\right]^{(k)}$$
(5)

where  $\xi_k (k = 1, 2, 3)$  are Majorana parameters since the Majorana interaction has been introduced to push the states with a mixed  $\pi \nu$  symmetry character to higher energies thereby at the same time reducing the possible F – spin admixing in low-lying states [12]. The energy levels are obtained by diagonalizing the Hamiltonian of eq.
(2) and then allowing the parameters ∈<sub>π</sub>, ∈<sub>ν</sub>, K, χ<sub>π</sub>, χ<sub>ν</sub> and C<sub>L</sub> to vary until a best fit to the experimental spectrum is obtained.

#### 3. Energy spectra

The values of the parameters of the transitional nuclei  $SU(5) \rightarrow O(6)$ of the Ru-isotopes employed in the hamaltonian of IBM-2 are displayed in Table (1).

Parameters	<sup>98</sup> Ru	<sup>100</sup> Ru	$^{102}Ru$	$^{104}Ru$	<sup>106</sup> Ru	$^{108}Ru$
N <sub>v</sub>	2	3	4	5	6	7
Ν <sub>π</sub>	3	3	3	3	3	3
E	0.935	0.910	0.865	0.760	0.690	0.660
k	-0.163	-0.155	-0.145	-0.140	-0.140	-0.140
$\chi_{\nu}$	-0.800	-1.000	-0.900	-0.900	-1.000	-0.800
χ <sub>π</sub>	0.400	0.400	0.400	0.400	0.400	0.400
$C_{0\nu}$	-0.950	-0.853	-0.760	-0.316	-0.110	-0.060
C <sub>2v</sub>	0.185	0.135	-0.100	-0.126	-0.070	-0.050
$C_{4\nu}$	-0.740	-0.238	-0.127	-0.075	-0.055	-0.050
$\xi_1$	0.100	0.100	0.100	0.100	0.100	0.100
ξ2	0.100	0.100	0.100	0.100	0.100	0.100
ξ3	0.100	0.100	0.100	0.100	0.100	0.100

Table (1)	: The hamiltonian	narameters of	IBM-2 for	Ry – isotopes
	. The nannitoman	parameters or	IDIVI-2 101	nu isotopes.

The calculated energy spectra of Ru-isotopes are plotted in Fig. (1) as a function of the neutron numbers. A detailed comparison of the ground, gamma and beta bands with experiment are shown in Figs (1a), (1b) and (1c), respectively. Figure (1a) shows a good agreement between the

calculated energies of  $2^+$ ,  $4^+$ ,  $6^+$  and  $8^+$  states and those of the experimental data while the state  $10^+$  deviates significantly from the data at  ${}^{98}Ru_{54}$  isotope. However, we should be careful in comparing theory with experiment, since all calculated states

have a collective nature, whereas some of the experimental states may have a particle-like structure. For example in  $^{98}Ru_{54}$  isotope, the particle-like structure of 10<sup>+</sup> state is confirmed by the presence of a maximum in the energies at  ${}^{100}Ru_{54}$ . Fig. (1b) shows that the calculated energy of  $3_1^+$  and  $5_1^+$  states are predicted too high by IBM-2. This is a consequence of the presence of a Majorana term  $M_{\pi v}$  in the Hamiltonian of IBM-2. The parameters of the Majorana force have chosen in such a way that it push up states that are not completely symmetric with respect to proton and neutron bosons. Fig. (c) shows that the experimental 0<sup>+</sup><sub>2</sub> states are very well described by the calculated result whereas, in general, the calculated  $2^+_3$ and  $4^+_3$  are in reasonable agreement with the experimental data in Ru-isotopes.

#### 4. Electromagnetic properties

The electric quadrupole transition operater  $\hat{T}(E2)$  of IBM-2 is given by [11]

$$\hat{T}(E2) = e_{\pi}\hat{Q}_{\pi}^{\chi} + e_{\nu}\hat{Q}_{\nu}^{\chi}$$
(6)

$$\hat{Q}_{\rho}^{\chi} = \left[\hat{d}^{+} \times \hat{\tilde{s}} + \hat{s}^{+} \times \hat{\tilde{d}}\right]_{\rho}^{(2)} + \chi_{\rho} \left[\hat{d}^{+} \times \hat{\tilde{d}}\right]_{\rho}^{(2)}$$
(7)

It has been used for calculating the E2 transition rates and the quadrupole moments of the first excited  $2^+$  states

$$\frac{B(E2;2_2^+ \to 0_1^+)}{B(E2;2_2^+ \to 2_1^+)}, \quad \frac{B(E2;3_1^+ \to 4_1^+)}{B(E2;3_1^+ \to 2_2^+)}, \quad \frac{B(E2;2_2^+ \to 2_1^+)}{B(E2;2_1^+ \to 0_1^+)} \text{ and } \frac{B(E2;4_1^+ \to 2_1^+)}{B(E2;2_1^+ \to 0_1^+)}$$

which are displayed in Fig. (3), are calculated and compared with those of

 $Q_{2_1^*}$  in Ru-isotopes. In the principle, the values of proton-boson  $e_{\pi}$  and neutron-boson  $e_{\nu}$  effective charges could be different from each other and different for each nucleus. In the present work, fixed values of  $e_{\pi} = e_{\nu} = 0.102 \ eb$  in IBM-2 has been used for a chain of Ru-isotopes.

The calculated  $B(E2; I_i \rightarrow I_f)$ 

transitions (the solid curves), in  $e^2b^2$ , is plotted in Fig. (2) as a function of neutron numbers of Ru-isotopes and compared with those of experimental data (the filled circles). The calculated  $B(E2,2_1^+ \rightarrow 0_1^+),$  $B(E2,4_1^+ \rightarrow 2_1^+)$ transitions of figures (2a), (2b), respectively, agree quite well with those of the experimental data and they show an increase in their values with the increasing of the neutron numbers since this behavior is in consistent with the experiment. In figure (2c), the  $B(E2,2^+_2 \rightarrow 2^+_1)$ transition demonstrates an agreement with that of the experimental data for N = 54 and 60, but overestimates the data for N = 56 and 62. It is obvious from figure (2d), that the calculated  $B(E2, 2_2^+ \rightarrow 0_1^+)$ transition underestimates the data. This discrepancy may be attributed to considering a fixed value of effective charge  $(e_{\pi} = e_{\nu} = 0.102 \text{ eb})$  in the boson E2 operator of eq. (6) for all Ru-isotopes.

For the sake of completeness, the other B(E2) properties such as the ratios

The quadrupole moments of the first excited  $2_1^+$  state  $Q_{2_1^+}$ for Ru-isotopes are also studied in this work and presented in Fig. (4). In this figure the calculated  $Q_{2_{1}^{+}}$ 15 represented by the solid curve. While the filled circles are those of the experimental, It is very clear that the general feature of these experimental data is an increase in the negative quadrupole moment with increasing the neutron number. Inspection of this figure provides an indication that the experimental data of the quadrupole moments of the first excited  $2^+_1$  state are very well described by the calculation of IBM-2 throughout all the considered Ru-isotopes. It is seen that the calculated  $Q_{2^+}$  of IBM-2 gives a remarkable agreement, in both behavior and magnitude, in comparison with those of experimental data.

The properties of the magnetic dipole operator such as the B(M1) transition and the magnetic dipole moment of the first excited  $2_1^+$  ( $\mu_{2_1^+}$ ) state as well as the  $\delta$ -mixing ratios are also studied by the present work of IBM-2. Here, the boson M1 operator,

$$\hat{T}(M1) = \sqrt{\frac{3}{4\pi}} \left( g_{\pi} \hat{L}^{\pi} + g_{\nu} \hat{L}^{\nu} \right)$$
(8)

is used to reproduce these properties. However, these properties are exclusively determined by the parameters of  $g_{\pi}$  and  $g_{\nu}$  factors. In this study a fixed values for  $g_{\pi}=0.25 \,\mu_N$  and  $g_{\nu}=0.085 \,\mu_N$  is chosen as a first choice to reproduce these properties throughout all Ru-isotopes under study. Since these values have been determined from the comparison between the calculated  $B(M1;2_2^+ \rightarrow 2_1^+)$  of IBM-2 and that of the experimental result in the <sup>104</sup>Ru-isotope [18].

The comparison between the calculated B(M1) transitions and  $\mu_{2^+}$  moments of IBM-2 model and those of the experimental data [14-18] is presented in Table (2). A clear picture could not be drawn for the properties of the B(M1) transition in the Ru-isotopes due to the lack of experimental data. Table (2) shows that the calculated  $\mu_{2^+}$  denoted by Th1, obtained using the first choice of  $g_{\pi} = 0.25 \,\mu_N$  and  $g_{\nu} = 0.085 \,\mu_N$ , are not in agreement with those of experimental data for all considered Ru – isotopes. An improvement results for the calculated  $\mu_{2^+}$  denoted by Th2 could be obtained due to adopting a second choice of  $g_{\pi}$  and  $g_{\nu}$  such as  $g_{\pi}=1.00 \,\mu_N$  and  $g_{\nu}=0.42 \,\mu_N$ . These values have been obtained from the comparison between the calculated magnetic dipole moments of the first excited state  $2_1^+$  and that of the experimental data in the  $^{102}Ru$  – isotope [17]. As it is seen from Table (2) that the experimental data of  $\mu_{2_1^+}$  are well explained by the calculated  $\mu_{2^+_1}$  of IBM-2 using the second choice of  $g_{\pi}$  and  $g_{\gamma}$ .

The  $\delta$  – mixing ratios in the considered Ru-isotopes is also studied here and defined as

$$\delta(E2/M1) = 0.832E_{\gamma} \times \Delta(E2/M1)$$
(9)

Where  $E_{\gamma}$  is in MeV and  $\Delta(E2/M1)$  is in  $eb/\mu_N$  and defined as

the ratio of the reduced E2 matrix element to the M1 matrix element, i.e.

$$\Delta(E2/M1) = \frac{\left\langle f \| \hat{T}(E2) \| i \right\rangle}{\left\langle f \| \hat{T}(M1) \| i \right\rangle}$$
(10)

In Tables (3) to (8), the comparison between the experimental  $\delta(E2/M1)$  mixing ratios [25,30-32] and those obtained by the present calculations of the IBM-2 using our first choice of  $g_{\pi}=0.25 \,\mu_N$  and  $g_{\nu}=0.085 \,\mu_N$  are

explored for all considered Ru-isotopes. In general, these Tables demonstrate that the absolute magnitudes of the calculated results for the  $\delta(E2/M1)$  mixing ratios are in reasonable agreement with those of experimental data. However, predicting the sign of these  $\delta(E2/M1)$  mixing ratios is a common problem in the IBM-2 model in spite of the reproduction of some of these  $\delta(E2/M1)$  mixing ratios correctly.

**Table (2):** The  $B(M1; I_i \rightarrow I_f)$  values, in the unit of  $(\mu_N^2)$ , and the magnetic dipole moments for the  $2_1^+$  states  $(\mu_{2_1^+})$ , in the unit of  $(\mu_N)$ , for Ru – isotopes obtained by IBM-2 model. The effective g-factors are taken as  $g_{\pi}=0.25 \,\mu_N$  and  $g_{\nu}=0.085 \,\mu_N$  for the calculations of B(M1) and  $\mu_{2_1^+}$  (Th1) and as  $g_{\pi}=1.00 \,\mu_N$  and  $g_{\nu}=0.42 \,\mu_N$  for the calculations of  $\mu_{2_1^+}$  (Th2). The experimental values for B(M1) and for  $\mu_{2_1^+}$  are taken from Refs [14-18].

$I_i \rightarrow I_f$	<sup>98</sup> Ru	<sup>100</sup> Ru	$^{102}Ru$	$^{104}Ru \ B(M1)$	$^{106}Ru B(M1)$	$^{108}Ru$
	<i>B</i> ( <i>M</i> 1)	<i>B</i> ( <i>M</i> 1)	<i>B</i> ( <i>M</i> 1)			
$l_1^+ \rightarrow 2_1^+$	0.0003	0.0007	0.0007	0.0009	0.0016	0.0006
$2^+_2 \rightarrow 2^+_1$	0.0036 Exp: 0.0033 ± 0.0006	0.0016 Exp: 0.0041± 0.007	0.0007 Exp: $\le 10^{-4}$	0.0004 Exp: 0.0004± 0.00005	0.0003	0.0002
$2^+_3 \rightarrow 2^+_1$	0.0075	0.0007	0.0002	0.0005	0.0004	0.0004
$2^+_4 \rightarrow 2^+_1$	0.0001	0.0086	0.0089	0.0075	0.0060	0.0006
$3^+_1 \rightarrow 2^+_1$	0.0001	0.0001	0.0001	0.0001	0.0001	0.0001
$3^+_2 \rightarrow 2^+_1$	0.0007	0.0005	0.0003	0.0003	0.0005	0.0002
$3^+_1 \rightarrow 2^+_2$	0.0031	0.0027	0.0007	0.0003	0.0005	0.0002
$\mu_{2_{1}^{+}}$	Th1: 0.1695 Th2: $0.7170$ Exp: $0.80 \pm 0.08$ $0.78 \pm 0.06$	$\begin{array}{ccc} Th1: & 0.1588\\ Th2: & 0.6708\\ & Exp:\\ 1.02\pm0.18\\ \end{array}$	$\begin{array}{ccc} \text{Th1:} & 0.1495 \\ \text{Th2} & :0.6468 \\ & \text{Exp:} \\ 0.69 \pm 0.042 \end{array}$	$\begin{array}{ccc} \text{Th1:} & 0.1407 & \text{Th2:} \\ 0.6158 & \text{Exp:} \\ & 0.82 \pm 0.20 \\ & 0.64 \pm 0.02 \end{array}$	Th1: 0.1313 Th2: 0.5828 Exp:	Th1: 0.1276 Th2: 0.5695 Exp: 0.54±0.06

**Table (3):** A comparison between the experimental  $\delta$  – mixing ratios and those obtained by the present calculations using the parameters  $e_{\pi} = e_{\nu} = 0.102 \ e.b$ ,  $g_{\pi} = 0.25 \ \mu_N$  and  $g_{\nu} = 0.085 \ \mu_N$  in the IBM-2 for

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the $^{98}Ru$ – isotope. The
experimentaldat are taken from Refs
[30,14].

Transitions	$\delta$ – mixing ratios	$\delta$ – mixing ratios
$(I_i \rightarrow I_f)$	Experiment	IBM-2
$2^+_2 \rightarrow 2^+_1$	$13.4_{-2.5}^{+3.9}$	0.903
$2^+_3 \rightarrow 2^+_1$		-0.389
$2^+_4 \rightarrow 2^+_1$		0.202
$3^+_1 \rightarrow 2^+_1$		1.886
$3^+_2 \rightarrow 2^+_1$		-0.002
$3_1^+ \rightarrow 2_2^+$	$0.4_{-0.3}^{+1.7}$	08.72
$1_1^+ \rightarrow 2_1^+$		-0.330

 $e_{\pi} = e_v = 0.102 \ e.b \,, \ g_{\pi} = 0.25 \ \mu_N$ 

and  $g_{\nu} = 0.085 \ \mu_N$  in the IBM-2 for

the  ${}^{100}Ru$  – isotope. The experimental dat are taken from Refs[15,16,31].

Transitions	$\delta$ – mixing	$\delta$ – mixi
	ratios	ng ratios
$(I_i \rightarrow I_f)$	(Experime	(IBM-2)
	nt)	
$2^+_2 \rightarrow 2^+_1$	$3.5 \pm 4$ ,	1.514
2	$2.4_{-1.2}^{+0.47}$	
$2^+_3 \rightarrow 2^+_1$	$0.22_{-0.6}^{+0.4}$	-0.751
$2^+_4 \rightarrow 2^+_1$		-0.0005
$3_1^+ \rightarrow 2_1^+$	$1.3_{-0.9}^{+0.4}$	1.335
$3^+_2 \rightarrow 2^+_1$		-0.105
$3_1^+ \rightarrow 2_2^+$		1.139
$l_1^+ \rightarrow 2_1^+$		-0.043

**Table (4):** A comparison between the experimental  $\delta$  – mixing ratios and those obtained by the present calculations using the parameters

**Table (5)**: A comparison between the experimental  $\delta$  – mixing ratios and those obtained by the present calculations using the parameters  $e_{\pi} = e_{\nu} = 0.102 \ e.b$ ,  $g_{\pi} = 0.25 \ \mu_N$  and  $g_{\nu} = 0.085 \ \mu_N$  in the IBM-2 for the <sup>102</sup>Ru – isotope. The experimentaldat are taken from Ref's [17,31].

Transitions	$\delta$ – mixing ratios Experiment	$\delta$ – mixing ratios IBM-2
$(I_i \rightarrow I_f)$		
$2^+_2 \rightarrow 2^+_1$	5 <sup>+2</sup> <sub>-3</sub>	2.172
$2^+_3 \rightarrow 2^+_1$	0.28 <sup>+0.3</sup> 0.3	-1.43
$2^+_4 \rightarrow 2^+_1$		-0.029
$3^+_1 \rightarrow 2^+_1$	-6.7 <sup>+0.9</sup> <sub>-0.7</sub>	2.225
$3^+_2 \rightarrow 2^+_1$	$-7.9^{+3.1}_{-1.4}$	0.246
$3^+_1 \rightarrow 2^+_2$	-7.2 ±1	2.341
$1_1^+ \rightarrow 2_1^+$		0.008

**Table (6):** A comparison between the experimental  $\delta$  – mixing ratios and

those obtained by the present calculations using the parameters

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$e_{\pi} = e_{\nu} = 0$	.102 <i>e.b</i> ,	$g_{\pi} = 0.25 \ \mu_N$
and $g_v = 0$	.085 $\mu_N$ in	the IBM-2 for
the	$^{104}Ru-isote$	ope. The
	aldat are ta	ken from Ref's
[18,31,25].		

Transitions	$\delta$ – mixing	$\delta$ – mi
$(I_i \rightarrow I_f)$	ratios	xing
	Experiment	ratios
		IBM-2
$2^+_2 \rightarrow 2^+_1$	$-8.5^{+2.5}_{-1.5}$	2.854
$2^+_3 \rightarrow 2^+_1$	$0.45 \pm 0.12$	-0.573
$2^+_4 \rightarrow 2^+_1$	$-0.03 \pm 0.04$	-0.070
$3^+_1 \rightarrow 2^+_1$	$-3.2 \pm 0.4$	3.111
$3^+_2 \rightarrow 2^+_1$	$0.12 \pm 0.10$	0.334
$3^+_1 \rightarrow 2^+_2$		3.565
$1^+_1 \rightarrow 2^+_1$		-0.043

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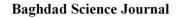
obtained by the present calculations using the parameters  $e_{\pi} = e_{\nu} = 0.102 \ e.b$ ,  $g_{\pi} = 0.25 \ \mu_N$  and  $g_{\nu} = 0.085 \ \mu_N$  in the IBM-2 for the <sup>106</sup>*Ru* – isotope. The experimental dat are taken from Ref's [19,20,32].

Transitions	$\delta$ – mixing	$\delta$ – mixi
$(I_i \rightarrow I_f)$	ratios	ng ratios
. ,.	Experiment	IBM-2
$2^+_2 \rightarrow 2^+_1$	$7.1^{+1.6}_{-11}$	3.245
$2^+_3 \rightarrow 2^+_1$	$0.24^{+0.13}_{0.12}$	0.104
$2^+_4 \rightarrow 2^+_1$		0.076
$3^+_1 \rightarrow 2^+_1$	-3.8 <sup>+0.9</sup> <sub>-1.6</sub>	3.428
$3^+_2 \rightarrow 2^+_1$		0.546
$3_1^+ \rightarrow 2_2^+$		3.061
$l_1^+ \rightarrow 2_1^+$		-0.098

**Table (8):** A comparison between the experimental  $\delta$  – mixing ratios and those obtained by the present calculations using the parameters  $e_{\pi} = e_{\nu} = 0.102 \ e.b$ ,  $g_{\pi} = 0.25 \ \mu_N$  and  $g_{\nu} = 0.085 \ \mu_N$  in the IBM-2 for the <sup>108</sup>*Ru* – isotope. The experimental dat are taken from Ref's [21,32].

Transitions	$\delta$ – mixing	$\delta$ – mixi
$(I_i \rightarrow I_f)$	ratios	ng ratios
	Experiment	IBM-2
$2^+_2 \rightarrow 2^+_1$	$4.3^{\rm +0.89}_{\rm -0.63}$	3.977
$2_3^+ \rightarrow 2_1^+$	$0.87 \pm 0.66$	-0.023
$2^+_4 \rightarrow 2^+_1$	$0.29^{\rm +0.11}_{\rm -0.14}$	0.206
$3_1^+ \rightarrow 2_1^+$		7.537
$3^+_2 \rightarrow 2^+_1$		0.784
$3^+_1 \rightarrow 2^+_2$	$-3.0^{+0.7}_{-1.4}$	3.700
$1_1^+ \rightarrow 2_1^+$	3	-0.272

Table (7): A comparison between the experimental  $\delta$  – mixing ratios and those



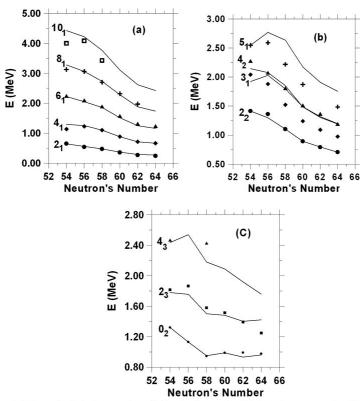
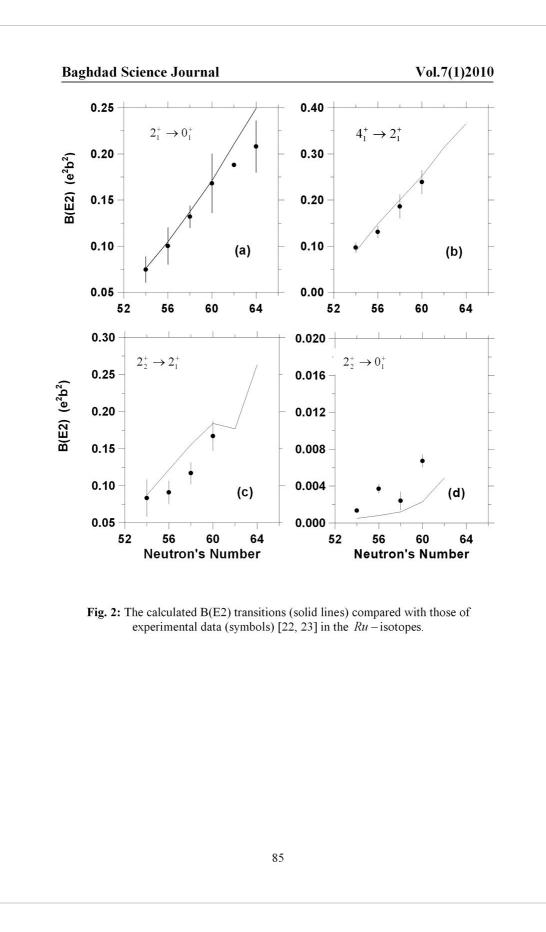
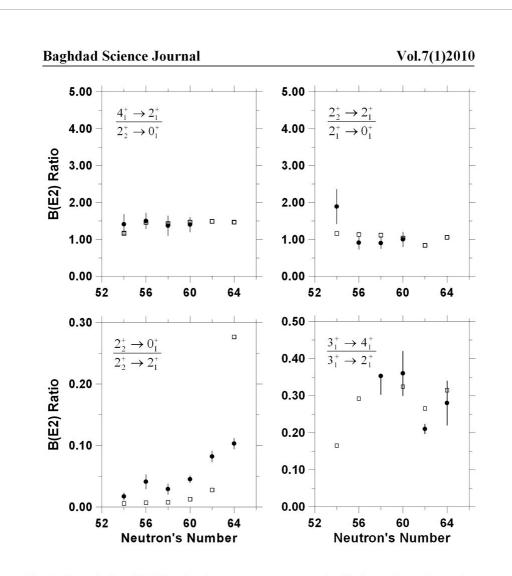


Fig. 1: The calculated energies of *Ru*-isotopes (solid lines) compared with those of experimental data (symbols) [14-21] for: (a) ground state band, (b) gamma state band and (c) beta state band.





**Fig. 3:** The calculated B(E2) ratios (open squares) compared with those of experimental data (solid circles) [24-27] in the *Ru* – isotopes.

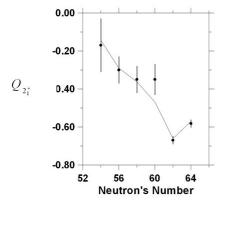


Fig. 4: The calculated quadrupole moments (the solid line) for the first excited  $2_1^+$  state compared with those of experimental data (solid circles) [23, 28, 29] in the Ru-isotopes.

## **Conclusions:**

The analysis performed in this study makes it possible to draw the following:

- 1. The low-lying experimental energy levels of the ground state bands in all Ru-isotopes are very well reproduced by those of calculated results of IBM-2 as seen in Fig. (1).
- 2. In general, the calculated results of IBM-2 the for B(E2) transitions in all considered Ru-isotopes show an increase in their values with the increasing of the neutron numbers since this behavior agree quite well with those of the experimental data. In addition, the calculated  $B(E2;2_2^+ \rightarrow 0_1^+)$  of IBM-2 is not in agreement with the experimental results all throughout considered Ru-isotopes. This discrepancy may be attributed to the considering a fixed value of effective charge.
- 3. The experimental quadrupole moments of the first excited  $2_1^+$  state  $Q_{2_1^+}$  are very good described by the calculations of IBM-2 throughout all considered Ru isotopes. Both the calculated and the experimental  $Q_{2_1^+}$  show a general feature of increasing their values in the negative quadrupole moment with increasing the neutron number.
- 4. We could not draw an explicit conclusion for the B(M1)transitions in the considered Ru-isotopes because of the lack of the experimental data in these isotopes. However, It is concluded that the properties of M1 operator are exclusively determined by the

parameters of  $g_{\pi}$  and  $g_{\nu}$  factors since using the choice of  $g_{\pi}=0.25 \,\mu_{N}$  and  $g_{\nu}=0.085 \,\mu_{N}$  in the calculations of IBM-2 produces results for the magnetic dipole moments  $\mu_{2^+}$  [denoted by Th1 in Table (2)] do not agree with the experiment throughout all considered Ru-isotopes while the choice of  $g_{\pi}=1.00 \mu_N$  and  $g_{\nu}=0.42 \,\mu_{N}$  gives results for  $\mu_{2^+}$  [denoted by Th2 in Table (2)] agree quite well with the experiment throughout all considered Ru-isotopes.

#### References

- Hicks S.F., Vanhoy J.R.,and Yates S.W., 2008.Fragmentation of mixedsymmetry excitations in stable even-even tellurium nuclei, Phys.Rev., C78, 54320
- Falih H., 2009. Mixed symmetry states and decays of odd-A Xe to I isotopes, Phys.Rev., C80, 14306.
- Genilloud L., Brown T., Warr N., Tolie J. and Yates S., 2001. Characterization of the 3phonon region Ru-100, Nucl.Phys., A683, 287.
- Gade A., Wiedmnover I., Meise H., Gelberg A. and Vonbrentano P., 2002.Decay properties of low-lying collectives states in Ba-132, Nucl.Phys., A697, 75.
- Pasternak A., Sasaki Y., Efimov A., Mikhajlov V., Shinohara N. and Liu Z., 2001.DSA lifetime measurements and structure of positive parity bands of X-120,

European Physical Joarnal, A9, 293.

- Saha A., Seth K., Casey L., Godman D., Stuart J. and Scholten O., 2001, Phys.Rev., C6302, 4309.
- Fransen C., Pietralla N., Dewald A., Gableske J., Lisetskiy A. and Werner V., 2001, Phys.Letts., B 506, 219.
- Saha A., Seth K., Casey L., Seth R., Stuart J. and Scholten O., 2001, Phys.Letts., B 132, 51.
- Carr J., Petrovich F., Philpott R., Scholten O. and Mcmanus H., 1985, Phys.Rev.Letts., 54, 11985.
- Fransen C. et. al., 2001.Identification of mixedsymmetry states in Mo-44, Acta Physica Polonica, B 32, 777.
- 11. Arima A. and Iachello F., 1981.Collective nuclear states as symmetric couplings of proton and neutron excitations, Ann.Rev.Nucl.Part.Sci., 31, 75.
- Sambataro M., Scholten O., Dieperink A. and Piccitto G., 1984.On magnetic dipole properties in the neutron-proton model, Nucl.Phys., A423, 333.
- Otsuka T., Arima A. and Iachello F., 1978.New symmetry in the sd model of nuclei the group o(6), Nucl.Phys., A 309, 1.
- Gelder P., Jacob E. and Frenne D., 1983, Nuclear Data Sheets, 39, 533.
- 15. Gelder P., Erenne D. and Jacobs E., 1974, Nucl Data Sheets, 11, 302.
- Samuelson L.E., Auble R.L. and Mcharris W.C., 1976, Nuclear Data Sheets, 19, 19.
- 17. Lipas P., Hammaren E. and Frenne D., 1982, Nuclear Data Sheets, 35, 451.

- Van Isacker P., Jacob E. and Frenne D., 1984, Nuclear Data Sheets, 41, 332.
- 19. Rachavan P., 1980, Nuclear Data Sheets, 30, 346.
- Frenne D., Gelder P. and Jacob E., 1988, Nuclear Data Sheets, 53, 78.
- Haese R.L., Bertrand F.H., 1982, Nuclear Data Sheets, 37, 292
- Raman et al., 1989, Atomic Data And Nuclear Data Tables, 42, 1, 15.
- 23. Bockisch A., Gelberg A., and Kaup U., 1979.Reorientation effect measurement and multiple coulomb excitation in  $^{102}Ru$ , Z.Physika., 292, 265.
- 24. Frenne D., et al., 1978.  $\beta^$ decay of  ${}^{102}Te$ , Physical Review C, 18, 1, 486.
- 25. Summer K., et al., 1978. Angular correlations of  $\gamma$  – ray transitions in  $^{104}Ru$ , Nuclear Physics, A308, 1.
- Summrer K., et al., 1980.Levels in <sup>106</sup>*Ru and* <sup>108</sup>*Ru*, Nuclear Physics, A339, 74.
- 27. Van P.,and Heyde K., 1982.Interpretation of the A=100 transitional region in the frame work of the IBM model, Physical Review C, 25, 1, 650.
- Landsberger S., et al., 1980.Quadrupole moments of the first excited states of <sup>96</sup>Ru,<sup>98</sup>Ru,<sup>100</sup>Ru,<sup>102</sup>Ru, and<sup>104</sup>Ru , Physical Review C, 121 2, 588.
- 29. Hirata H., Salem S.,and Dietzsch O., 1998.Electromagnetic properties of the first 2<sup>+</sup><sub>1</sub> excited states in <sup>100,102,104</sup>*Ru*, Phys.Rev., C57, 76.

- 30. Stngh B., and Taylor W., 1970.Directional correlation and multipole mixing of the gamma transitions in  $^{102}Ru$ , Nuclear Physics, A155, 70.
- 31. Krone K.S., 1984. Coulomb excitation of states in the evenmass ruthenlum nuclei with

- $^{16}O$  and  $^{4}He$  ion, Physical Review C, 10, 3,1197.
- 32. Stachei J., Broden K., and Eriksen D., 1984. The collective structure of <sup>106,108</sup>*Ru*, Z.Phys. Atomic and Nuclei, 316, 105

# دراسة الخواص النووية لنظائر Ru استخدام IBM

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## الخلاصه:

لقد تم استخذام انموذج البوزونات المتفاعله (IBM-2) لعمل دراسة تخطيطية لنظائر الروثنيوم (Ru) الموثر (Ru) المتواجدة ضمن منطقة العدد الكتلي 00 = A و العدد النيوتروني  $54 \ge N \le 54 \ge 100$ . لقد تم ايجاد اعلومات المؤثر الموثر واليهاملتوني والتي اعطت نتائج مقبولة لطاقات التهيج مقارنة مع النتائج العملية. لقد تم استخذام قيم ثابتة لكل من الشحنات الموثرة ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$  الموثرة ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$ ) جميع المؤثرة للأعلومتين ( $g_v = 0.42 \ \mu_N$  و  $n = 1.0 \ \mu_N$ ) الموثرة ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$ ) الموثرة ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$ ) الموثرة المؤثرة المؤثرة الموثرة الموثين ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$  ونميتين ( $g_v = 0.42 \ \mu_N$  والترة ( $g_v = 0.102 \ e.b$ ) الموثرة المؤثرة الموثرة الموثرة المؤثرة المؤثرة المؤثرة الموثرة الموثين ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$  والتر الموثرة ( $g_v = 0.42 \ \mu_N$  و  $g_\pi = 1.0 \ \mu_N$  والترة ( $g_v = 0.42 \ \mu_N$  والترة ( $g_v = 0.42 \ \mu_N$  والترة ( $g_v = 0.102 \ e.b$ ) والترة ( $g_v = 0.102 \ e.b$ ) الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.42 \ \mu_N$  والترة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثرة ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والترة الموثر ( $g_v = 0.102 \ e.b$ ) والتر ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.b$ ) والترة ( $g_v = 0.102 \ e.b$ ) والتر ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.b$ ) والتر ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.b$ ) والترم ( $g_v = 0.102 \ e.$