

SBOA: A Novel Heuristic Optimization Algorithm

Qi Diao*¹ , **Apri Junaidi**² , **WengHowe Chan**² , **Azland Mohd Zain**² ,
Hao long Yang³ 

¹Faculty of Artificial Intelligence, Zhejiang Dongfang Polytechnic, Wenzhou, 32500, China.

²Faculty of Computing, Universiti Teknologi Malaysia, 81310, Skudai, Johor, Malaysia.

³Boston University, Massachusetts, 02215, America.

*Corresponding Author.

ICAC2023: The 4th International Conference on Applied Computing 2023.

Received 30/09/2023, Revised 10/02/2024, Accepted 12/02/2024, Published 25/02/2024



© 2022 The Author(s). Published by College of Science for Women, University of Baghdad.

This is an Open Access article distributed under the terms of the [Creative Commons Attribution 4.0 International License](#), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Abstract

A new human-based heuristic optimization method, named the Snooker-Based Optimization Algorithm (SBOA), is introduced in this study. The inspiration for this method is drawn from the traits of sales elites—those qualities every salesperson aspires to possess. Typically, salespersons strive to enhance their skills through autonomous learning or by seeking guidance from others. Furthermore, they engage in regular communication with customers to gain approval for their products or services. Building upon this concept, SBOA aims to find the optimal solution within a given search space, traversing all positions to obtain all possible values. To assesses the feasibility and effectiveness of SBOA in comparison to other algorithms, we conducted tests on ten single-objective functions from the 2019 benchmark functions of the Evolutionary Computation (CEC), as well as twenty-four single-objective functions from the 2022 CEC benchmark functions, in addition to four engineering problems. Seven comparative algorithms were utilized: the Differential Evolution Algorithm (DE), Sparrow Search Algorithm (SSA), Sine Cosine Algorithm (SCA), Whale Optimization Algorithm (WOA), Butterfly Optimization Algorithm (BOA), Lion Swarm Optimization (LSO), and Golden Jackal Optimization (GJO). The results of these diverse experiments were compared in terms of accuracy and convergence curve speed. The findings suggest that SBOA is a straightforward and viable approach that, overall, outperforms the aforementioned algorithms.

Keywords: autonomous learning, Evolutionary Computation, Heuristic optimization method, Single objective function, search space.

Introduction

In recent years, more and more researchers have focused on optimization problems, and proposed lots of algorithms. Their inspirations originate from different thoughts such as phenomenon, behaviors, simulation process, and so on. The structures of algorithms are simple and confirm that they are

feasible and efficient to solve optimization problems. These optimization algorithms are divided into two categories: metaheuristic algorithms, heuristic algorithm.

Metaheuristic algorithms are divided into four categories: evolutionary algorithms, swarm algorithms, chemical & physical algorithms, and human-based algorithms^{1,2}. The well-known algorithms are Genetic Algorithm (GA)³, Differential Evolution Algorithm (DE)⁴, Snake Optimizer (SO)⁵, Sparrow Search Algorithm (SSA)⁶, Golden jackal optimization (GJO)⁷, Pelican Optimization Algorithm (POA)⁸, Sine cosine algorithm (SCA)⁹, Whale Optimization Algorithm (WOA)¹⁰, Grey Wolf Optimizer (GWO)¹¹, Thermal Exchange Optimization (TEO)¹², Teaching-learning-based optimization (TLBO)¹³, Student psychology based optimization algorithm (SPBO)¹⁴, Ant Colony Optimization (ACO)¹⁵, Simulate Anneal Arithmetic¹⁶ (SAA), Particle Swarm optimization (PSO)¹⁷, Butterfly Optimization Algorithm(BOA)¹⁸, and so on.

Heuristic algorithms provide footing stone for metaheuristic algorithms, and metaheuristic algorithms are included in heuristic algorithms. The commonness of metaheuristic algorithms and heuristic algorithms lies in obtaining the optimal solution, the difference is the degree of greed, namely heuristic algorithm is easy to fall into local solution.

SBOA

This section includes the inspiration and the mathematical model of SBOA.

Inspiration source

The layout of snooker is shown in **Error!** **Reference source not found.** As everyone knows, if any player wants to win, he/she must make a good score. The highest score is 147, namely player must get 74 points at least. In a word, the number of cue balls contacting object balls must be more. It is said that one careless move loses the whole game. Therefore, players must maintain the initiative throughout the game. On one hand, players get score by offensive strategy. On the other hand, the player stops the opponent from scoring by defensive strategy, namely the cue ball is reasonably controlled by player, and create chances for score. can see from above; offensive strategy is an overall thinking and defensive strategy is a local thinking. The aim is to make a good score whether offensive

strategy or defensive strategy. Thus, the play rules can be used to solve optimization problems.

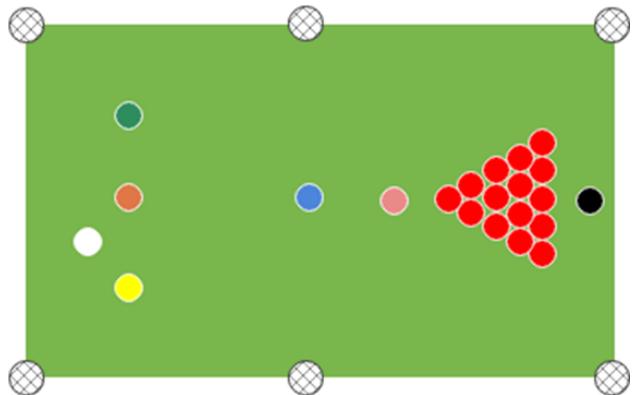


Figure 1. The layout of snooker.

Mathematical model

The thought about SBOA is simple, the structure is also simple. In the beginning of the search, the first kickoff result is produced by using Eq.1.

First, SBOA starts by generating a random population in uniform distribution to begin, including the cue ball and other balls. Based on this idea, the cue ball is considered as the best individual, its position that contacting object balls is very important. The initial population can be obtained using Eq.1.

$$X_i = X_{\min} + \text{rand} * (X_{\max} - X_{\min}) \quad 1$$

Where X_i is the position of all balls, rand is a random number between 0 and 1, and X_{\min} , X_{\max} are the lower and upper bounds of the problem respectively.

The best solution is shown using Eq.2.

$$\text{Best}X = \min(X_i), i = 1, 2, \dots, N \quad 2$$

Where N is the number of the first retrieval result.

Snooker as a sport with two players, is divided into two phases as follow:

(1) Attack phase

In the attack phase, the cue ball is contacted by other balls, a red ball then a colored ball. Alternating like this until a player wins. Therefore, the process is what the cue ball contacts other balls

so that has a good score. The process of Learning from colleagues is calculated using Eq. 3.

$$X_{i,new} = X_i + A \times \text{rand}(-1,1) \times (X_{best} - X_i)$$

$$A = \exp\left(\frac{t-10T}{T}\right)$$

3

Where X_{best} is the position of the cue ball, $\text{rand}(0, 1)$ is random vectors in intervals [-1, 1]. A presents offensive ability that adapting to the game.

(2) Defensive phase

In defensive phase, the cue ball can be docked two balls, cushion, or around snookered ball/balls. The aim is to prevent the opponent from winning or scoring when a player has no scoring advantage. Thus, the process is simulated using Eq.4.

$$X_{i,new} = X_i + B \times \text{rand}(0,1) \times (X_{best} - X_i)$$

$$B = 2\sin(\text{rand} + \frac{\pi t}{4T}) \times e^{\frac{t-T}{T}}$$

4

Where $\text{rand}(0, 1)$ is random vectors in intervals [0, 1], B presents defensive ability of players.

In the process, players usually have snooker according to the remaining balls on the billiard

Experiment and Result

In this subsection, the performance of the SBOA Test is divided into three parts and has different benchmark functions obtained from CEC 2019 and

table. Therefore, searching for the best one (ball) using Eq.5.

$$X_{i,new} = \begin{cases} X_j + \text{rand} * (X_i - X_j), & f(X_i) < f(X_j) \\ X_i + \text{rand} * (X_j - X_i), & f(X_j) < f(X_i) \end{cases}$$

5

Where $f(X_i)$ is the fitness of position X_i , $f(X_j)$ is the fitness of position X_j .

The pseudo-code of SBOA is shown in **Error! Reference source not found..**

Table 1. pseudo-code of SBOA

Algorithm: SBOA

```

1: Initialize Problem Setting
2: Initialize the population randomly
3: Calculate objective function using Eqs.2,
4: for t=1 to T
5:   phase1: Attack phase
6:   for i=1 to N
7:     Perform exploration phase using Eqs.3
8:   End
9:   phase2: Defensive phase
10:  for j=1 to N
11:    Perform exploration phase using Eqs.4, Eqs.5
12:  End
13: Return best solution
14: End

```

CEC 2022. Each algorithm is performed 30 times, and parameter settings are shown in Table 2.

Table 2. Experiments parameters settings

| Algorithm | Parameter name | Value |
|-----------|--|-------|
| Public | Population size | 30 |
| | Dim | 30 |
| | Max number of iteration Scaling Factor | 500 |
| DE | Crossover probability | 0.5 |
| SCA | a (constant) | 2 |
| WOA | Convergence parameter (a) | |
| | r is a random vector in the interval [0, 1] | |
| | I is a random number in [-1, 1] | |
| LSO | β (Proportion of adult lions) | |
| SSA | ST (threshold) | 0.6 |
| | PD (Proportion of discoverers) | 0.7 |
| | SD (Aware of the proportion of dangerous sparrows) | 0.2 |

| | | |
|-----|--|-------|
| GJO | c1(constant) | 1.5 |
| | r1(Random Number Based on Levy Distribution) | 0.05. |
| BOA | p (Global flight probability) | 0.8 |
| | c (constant) | 0.1 |
| | a (Fragrance concentration index) | 0.01 |

Result on CEC 2019

In this subsection, have used 10 objective functions obtained from CEC 2019.

Table 1 shows the CEC 2019 summary of test functions include functions, opt, D, search range.

Table 1. Benchmark functions of the CEC2019

| No. | Functions | Opt | D | Search Range |
|-----|--|-----|----|-----------------|
| 1 | Storn's Chebyshev Polynomial Fitting Problem | 1 | 9 | [-8192, 8192] |
| 2 | Inverse Hilbert Matrix Problem | 1 | 16 | [-16384, 16384] |
| 3 | Lennard-Jones Minimum Energy Cluster | 1 | 18 | [-4, 4] |
| 4 | Rastrigin's Function | 1 | 10 | [-100, 100] |
| 5 | Griewangk's Function | 1 | 10 | [-100, 100] |
| 6 | Weierstrass Function | 1 | 10 | [-100, 100] |
| 7 | Modified Schwefel's Function | 1 | 10 | [-100, 100] |
| 8 | Expanded Schaffer's F6 Function | 1 | 10 | [-100, 100] |
| 9 | Happy Cat Function | 1 | 10 | [-100, 100] |
| 10 | Ackley Function | 1 | 10 | [-100, 100] |

Comparison Result

Table 2 shows the results of SBOA and other seven comparative algorithms (DE, SCA, WOA, LSO, SSA, GJO and BOA) in terms of mean (average), best (min), worst (max), median, and std. From Error! Reference source not found., can see that

SBOA outperforms other algorithms overall. SBOA has the best Mean results in 7 functions of all functions and ranked second in 1 function whereas it ranked fifth in other 2 functions.

Table 2. The comparison results 10 functions using CEC2019

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|----|------|----------|----------|----------|----------|----------|----------|----------|
| F1 | Min | 6.62E+02 | 4.11E+04 | 1.00E+00 | 6.79E+04 | 1.00E+00 | 1.00E+00 | 1.67E+00 |
| | Mean | 6.06E+05 | 1.91E+07 | 3.47E+02 | 1.49E+07 | 1.00E+00 | 1.00E+00 | 1.00E+00 |
| | Max | 4.96E+06 | 2.08E+08 | 4.16E+03 | 5.35E+07 | 1.00E+00 | 1.00E+00 | 1.00E+00 |
| | Std | 1.18E+06 | 4.96E+07 | 1.03E+03 | 1.29E+07 | 0.00E+00 | 1.00E+00 | 0.00E+00 |
| F2 | Min | 2.04E+02 | 2.86E+02 | 4.44E+00 | 3.85E+03 | 4.94E+00 | 4.97E+00 | 5.00E+00 |
| | Mean | 1.63E+03 | 5.00E+03 | 1.17E+02 | 7.00E+03 | 5.00E+00 | 5.00E+00 | 5.00E+00 |
| | Max | 3.64E+03 | 1.34E+04 | 5.58E+02 | 1.31E+04 | 5.00E+00 | 5.00E+00 | 6.83E+03 |
| | Std | 9.54E+02 | 3.85E+03 | 1.65E+02 | 2.28E+03 | 1.48E-02 | 4.97E+00 | 0.00E+00 |
| F3 | Min | 1.00E+00 | 4.61E+00 | 1.39E+00 | 1.91E+00 | 5.08E+00 | 1.54E+00 | 4.23E+00 |
| | Mean | 1.87E+00 | 9.01E+00 | 4.18E+00 | 5.59E+00 | 6.48E+00 | 4.99E+00 | 5.71E+00 |
| | Max | 6.71E+00 | 1.23E+01 | 8.35E+00 | 9.71E+00 | 7.74E+00 | 8.05E+00 | 7.46E+00 |
| | Std | 1.20E+00 | 2.10E+00 | 2.38E+00 | 2.29E+00 | 7.95E-01 | 1.54E+00 | 9.01E-01 |
| F4 | Min | 8.96E+00 | 1.39E+01 | 2.11E+01 | 2.98E+01 | 4.49E+01 | 9.56E+00 | 2.99E+01 |
| | Mean | 2.95E+01 | 3.42E+01 | 3.29E+01 | 6.18E+01 | 8.95E+01 | 4.86E+01 | 7.43E+01 |
| | Max | 4.78E+01 | 6.63E+01 | 4.61E+01 | 1.02E+02 | 1.10E+02 | 7.78E+01 | 1.30E+02 |

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA | |
|----|------|----------|----------|----------|----------|----------|----------|----------|----------|
| F5 | Std | 1.20E+01 | 1.47E+01 | 8.80E+00 | 2.14E+01 | 1.46E+01 | 9.56E+00 | 2.55E+01 | 7.00E+00 |
| | Min | 1.07E+00 | 1.01E+00 | 1.65E+00 | 1.68E+00 | 7.22E+01 | 1.52E+00 | 3.27E+01 | 5.19E+00 |
| | Mean | 1.83E+00 | 3.87E+00 | 5.30E+00 | 2.32E+00 | 1.21E+02 | 1.93E+00 | 6.88E+01 | 9.93E+00 |
| | Max | 4.33E+00 | 3.51E+01 | 3.16E+01 | 3.49E+00 | 1.61E+02 | 2.63E+00 | 1.19E+02 | 1.94E+01 |
| | Std | 7.53E-01 | 7.75E+00 | 6.87E+00 | 4.76E-01 | 2.44E+01 | 1.52E+00 | 2.35E+01 | 4.05E+00 |
| F6 | Min | 2.66E+00 | 1.74E+00 | 2.63E+00 | 4.66E+00 | 7.03E+00 | 3.54E+00 | 7.85E+00 | 5.98E+00 |
| | Mean | 5.70E+00 | 6.13E+00 | 4.38E+00 | 8.91E+00 | 9.01E+00 | 7.92E+00 | 9.69E+00 | 7.83E+00 |
| | Max | 9.18E+00 | 1.49E+01 | 7.62E+00 | 1.22E+01 | 1.09E+01 | 1.05E+01 | 1.21E+01 | 1.05E+01 |
| | Std | 1.54E+00 | 2.62E+00 | 1.29E+00 | 1.84E+00 | 9.36E-01 | 3.54E+00 | 9.94E-01 | 1.33E+00 |
| | Min | 4.31E+02 | 3.51E+02 | 2.66E+02 | 5.30E+02 | 1.51E+03 | 5.07E+02 | 1.31E+03 | 8.73E+02 |
| F7 | Mean | 9.51E+02 | 1.53E+03 | 1.20E+03 | 1.34E+03 | 1.93E+03 | 1.10E+03 | 1.75E+03 | 1.64E+03 |
| | Max | 1.59E+03 | 2.58E+03 | 2.04E+03 | 2.24E+03 | 2.19E+03 | 1.59E+03 | 2.18E+03 | 2.02E+03 |
| | Std | 2.98E+02 | 4.95E+02 | 4.23E+02 | 3.95E+02 | 1.68E+02 | 5.07E+02 | 2.51E+02 | 2.25E+02 |
| | Min | 2.65E+00 | 4.10E+00 | 3.08E+00 | 4.20E+00 | 4.53E+00 | 4.34E+00 | 4.02E+00 | 3.60E+00 |
| | Mean | 3.96E+00 | 4.97E+00 | 4.14E+00 | 4.70E+00 | 4.88E+00 | 4.78E+00 | 4.76E+00 | 4.50E+00 |
| F8 | Max | 4.53E+00 | 5.44E+00 | 5.00E+00 | 5.04E+00 | 5.15E+00 | 5.08E+00 | 5.36E+00 | 5.08E+00 |
| | Std | 4.45E-01 | 3.39E-01 | 4.30E-01 | 2.62E-01 | 1.71E-01 | 4.34E+00 | 3.23E-01 | 3.20E-01 |
| | Min | 1.09E+00 | 1.04E+00 | 1.10E+00 | 1.19E+00 | 3.12E+00 | 1.16E+00 | 1.59E+00 | 1.36E+00 |
| | Mean | 1.25E+00 | 1.42E+00 | 1.29E+00 | 1.45E+00 | 4.37E+00 | 1.48E+00 | 3.36E+00 | 1.62E+00 |
| | Max | 1.44E+00 | 3.32E+00 | 1.49E+00 | 1.81E+00 | 5.67E+00 | 2.03E+00 | 5.18E+00 | 2.00E+00 |
| F9 | Std | 9.68E-02 | 4.13E-01 | 1.06E-01 | 1.44E-01 | 6.25E-01 | 1.16E+00 | 7.89E-01 | 1.63E-01 |
| | Min | 4.03E+00 | 2.13E+01 | 5.96E+00 | 2.11E+01 | 2.00E+01 | 2.11E+01 | 2.11E+01 | 2.13E+01 |
| | Mean | 2.01E+01 | 2.16E+01 | 2.05E+01 | 2.13E+01 | 2.14E+01 | 2.12E+01 | 2.15E+01 | 2.15E+01 |
| | Max | 2.16E+01 | 2.20E+01 | 2.16E+01 | 2.15E+01 | 2.16E+01 | 2.15E+01 | 2.17E+01 | 2.17E+01 |
| | Std | 3.92E+00 | 1.40E-01 | 3.76E+00 | 1.05E-01 | 2.80E-01 | 2.11E+01 | 1.51E-01 | 1.01E-01 |

Table 3 shows the Wilcoxon rank sum test results for SBOA against other algorithms. From this table, can see that most P values are less than 0.05, and

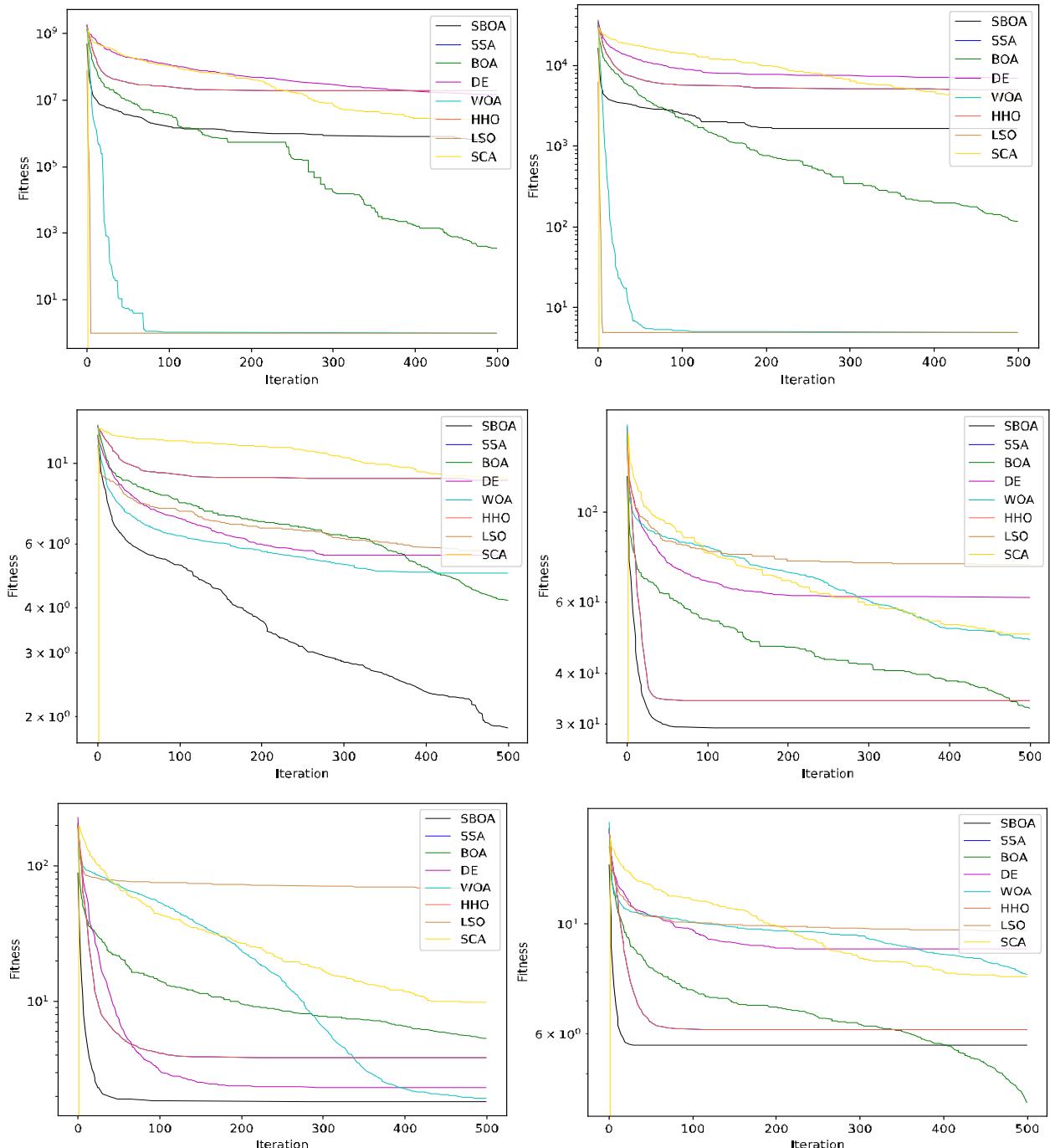
the smaller of the values, the better of these algorithms.

Table 3. Wilcoxon rank sum test results for SBOA against other algorithms CEC2019

| Function | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|----------|----------|----------|----------|----------|----------|----------|----------|
| F1 | 8.36E-04 | 9.17E-08 | 1.20E-06 | 8.01E-09 | 8.01E-09 | 8.01E-09 | 2.08E-01 |
| F3 | 2.14E-03 | 1.43E-07 | 6.80E-08 | 1.13E-08 | 6.68E-08 | 8.01E-09 | 4.17E-05 |
| F4 | 4.07E-11 | 6.52E-07 | 2.03E-09 | 4.57E-09 | 1.96E-10 | 4.61E-10 | 4.07E-11 |
| F5 | 3.65E-01 | 4.90E-01 | 6.67E-06 | 2.22E-04 | 1.06E-07 | 6.92E-07 | 5.17E-06 |
| F6 | 1.64E-01 | 5.25E-05 | 6.87E-04 | 2.23E-02 | 6.80E-08 | 6.80E-08 | 6.80E-08 |
| F7 | 4.83E-01 | 9.52E-04 | 9.06E-08 | 5.46E-06 | 6.12E-10 | 9.92E-11 | 3.32E-06 |
| F8 | 3.57E-06 | 1.22E-02 | 1.68E-04 | 3.51E-02 | 3.69E-11 | 2.15E-10 | 1.17E-09 |
| F9 | 5.07E-10 | 1.86E-01 | 1.55E-09 | 1.61E-10 | 3.34E-11 | 3.50E-09 | 8.20E-07 |
| F10 | 3.15E-02 | 1.33E-01 | 3.52E-07 | 2.28E-05 | 3.02E-11 | 3.02E-11 | 7.39E-11 |

Error! Reference source not found. show 10 convergence curves. From these convergence curves of all functions, it is seen that SBOA has

obvious superiority than other algorithms in 7 functions, the second-best of 1 other function whereas it ranked fifth in other 2 functions.



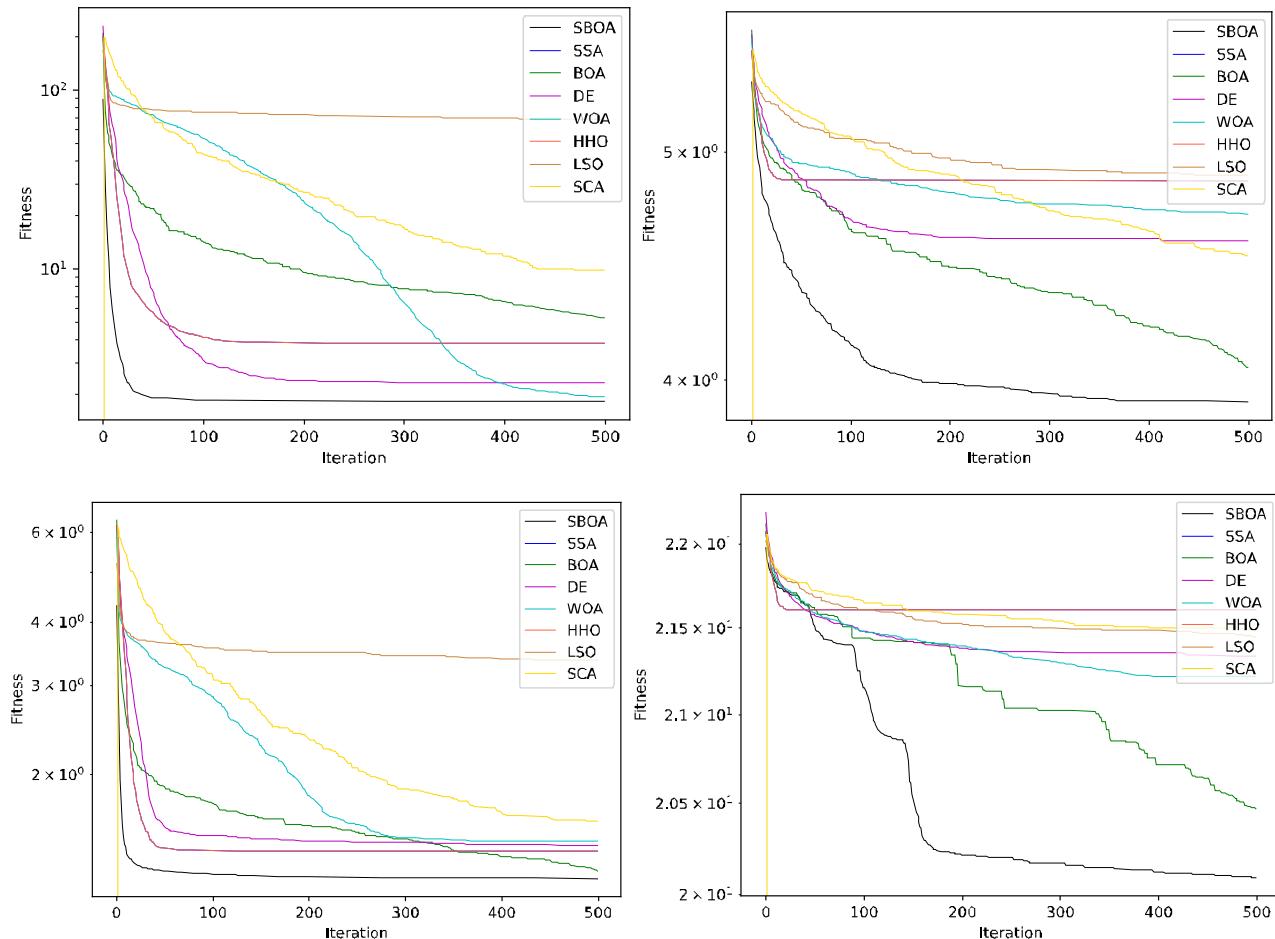


Figure 2. Convergence curve of some functions from F1–F10 for all algorithms CEC2019.

Result on CEC 2022

Table 4. Summary of the CEC 2022 test **functions** shows the CEC 2022 summary of test functions.

In this subsection, have used 12 objective benchmark functions obtained from CEC 2022.

Table 4. Summary of the CEC 2022 test functions

| Functions | No. | Functions | Opt |
|-----------------------|-----|---|------|
| Unimodal Functions | 1 | Shifted and full Rotated Zakharov Function | 300 |
| | 2 | Shifted and full Rotated Rosenbrock's Function | 400 |
| Basis Functions | 3 | Shifted and full Rotated Expanded Scaffer's F6 Function | 600 |
| | 4 | Shifted and \full Rotated Non-Continuous Rastrigin's Function | 800 |
| Hybrid Functions | 5 | Shifted and full Rotated Levy Function | 900 |
| | 6 | Hybrid Function 1 (N=3) | 1800 |
| Composition Functions | 7 | Hybrid Function 2 (N=6) | 2000 |
| | 8 | Hybrid Function 3 (N=5) | 2200 |
| Composition Functions | 9 | Composition Function 1 (N=5) | 2300 |
| | 10 | Composition Function 2 (N=4) | 2400 |
| | 11 | Composition Function 3 (N=5) | 2600 |
| | 12 | Composition Function 4 (N=6) | 2700 |

Search Range: [-100,100]^D

Comparison results

Table 5, Error! Reference source not found. show the results of SBOA and other seven comparative algorithms (DE, SCA, WOA, LSO, SSA, GJO and BOA) in terms of mean (average), best (min), worst (max), median, and std CEC 2022 and Dim=10.

And Dim=20. It is seen that SBOA has the best Mean results in 11 functions from all functions at least. So it has obvious superiority to other algorithms.

Table 5. The comparison results 12 functions using CEC 2022 and Dim=10

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA | |
|-----|------|----------|----------|----------|----------|----------|----------|----------|----------|
| F1 | Min | 3.35E+02 | 5.22E+02 | 6.44E+03 | 7.74E+02 | 8.49E+03 | 6.16E+03 | 5.08E+02 | 2.56E+03 |
| | Mean | 1.22E+03 | 1.22E+04 | 2.44E+04 | 2.47E+03 | 1.37E+04 | 8.76E+03 | 4.70E+03 | 6.58E+03 |
| | Max | 2.95E+03 | 7.43E+04 | 3.84E+04 | 5.74E+03 | 2.75E+04 | 1.05E+04 | 9.10E+03 | 9.08E+03 |
| | Std | 7.64E+02 | 2.23E+04 | 1.06E+04 | 1.39E+03 | 6.70E+03 | 6.16E+03 | 3.06E+03 | 2.16E+03 |
| F2 | Min | 4.00E+02 | 4.01E+02 | 4.01E+02 | 4.37E+02 | 5.14E+02 | 4.03E+02 | 4.01E+02 | 1.01E+03 |
| | Mean | 4.17E+02 | 4.23E+02 | 4.71E+02 | 4.74E+02 | 1.36E+03 | 4.84E+02 | 4.53E+02 | 2.41E+03 |
| | Max | 4.74E+02 | 5.71E+02 | 7.32E+02 | 5.31E+02 | 3.92E+03 | 7.42E+02 | 5.24E+02 | 4.25E+03 |
| | Std | 2.46E+01 | 3.60E+01 | 8.89E+01 | 1.82E+01 | 7.66E+02 | 4.03E+02 | 2.78E+01 | 9.37E+02 |
| F3 | Min | 6.00E+02 | 6.00E+02 | 6.18E+02 | 6.11E+02 | 6.26E+02 | 6.11E+02 | 6.01E+02 | 6.27E+02 |
| | Mean | 6.03E+02 | 6.10E+02 | 6.40E+02 | 6.21E+02 | 6.43E+02 | 6.46E+02 | 6.09E+02 | 6.45E+02 |
| | Max | 6.12E+02 | 6.30E+02 | 6.66E+02 | 6.30E+02 | 6.59E+02 | 6.65E+02 | 6.36E+02 | 6.57E+02 |
| | Std | 3.91E+00 | 7.77E+00 | 1.27E+01 | 4.83E+00 | 9.36E+00 | 6.11E+02 | 8.44E+00 | 7.76E+00 |
| F4 | Min | 8.11E+02 | 8.09E+02 | 8.22E+02 | 8.28E+02 | 8.26E+02 | 8.18E+02 | 8.12E+02 | 8.34E+02 |
| | Mean | 8.19E+02 | 8.40E+02 | 8.44E+02 | 8.47E+02 | 8.49E+02 | 8.32E+02 | 8.27E+02 | 8.54E+02 |
| | Max | 8.30E+02 | 8.90E+02 | 9.01E+02 | 8.59E+02 | 8.63E+02 | 8.54E+02 | 8.46E+02 | 8.74E+02 |
| | Std | 4.27E+00 | 1.86E+01 | 1.78E+01 | 7.56E+00 | 8.22E+00 | 8.18E+02 | 9.44E+00 | 8.44E+00 |
| F5 | Min | 9.00E+02 | 9.00E+02 | 1.01E+03 | 9.50E+02 | 1.02E+03 | 1.11E+03 | 9.02E+02 | 1.12E+03 |
| | Mean | 9.37E+02 | 1.40E+03 | 1.63E+03 | 1.07E+03 | 1.38E+03 | 1.41E+03 | 1.02E+03 | 1.40E+03 |
| | Max | 1.08E+03 | 3.27E+03 | 2.77E+03 | 1.36E+03 | 1.77E+03 | 1.49E+03 | 1.64E+03 | 1.79E+03 |
| | Std | 4.25E+01 | 5.98E+02 | 4.71E+02 | 1.05E+02 | 1.73E+02 | 1.11E+03 | 1.46E+02 | 1.64E+02 |
| F6 | Min | 1.83E+03 | 1.97E+03 | 2.44E+03 | 2.46E+05 | 1.29E+06 | 1.88E+03 | 4.36E+03 | 2.82E+06 |
| | Mean | 2.21E+03 | 5.17E+05 | 6.53E+03 | 5.07E+06 | 7.26E+07 | 2.85E+03 | 1.29E+04 | 1.55E+08 |
| | Max | 4.54E+03 | 1.42E+07 | 2.50E+04 | 1.95E+07 | 3.64E+08 | 5.78E+03 | 5.59E+04 | 9.69E+08 |
| | Std | 5.96E+02 | 2.60E+06 | 4.22E+03 | 4.83E+06 | 9.15E+07 | 1.88E+03 | 1.02E+04 | 2.30E+08 |
| F7 | Min | 3.10E+03 | 3.09E+03 | 3.11E+03 | 3.10E+03 | 3.12E+03 | 3.13E+03 | 3.09E+03 | 3.12E+03 |
| | Mean | 3.10E+03 | 3.11E+03 | 3.15E+03 | 3.11E+03 | 3.15E+03 | 3.22E+03 | 3.11E+03 | 3.19E+03 |
| | Max | 3.12E+03 | 3.17E+03 | 3.25E+03 | 3.11E+03 | 3.24E+03 | 3.33E+03 | 3.13E+03 | 3.30E+03 |
| | Std | 7.95E+00 | 2.41E+01 | 4.57E+01 | 2.82E+00 | 4.37E+01 | 3.13E+03 | 1.52E+01 | 5.95E+01 |
| F8 | Min | 2.20E+03 | 2.22E+03 | 2.22E+03 | 2.23E+03 | 2.23E+03 | 2.23E+03 | 2.22E+03 | 2.23E+03 |
| | Mean | 2.22E+03 | 2.23E+03 | 2.24E+03 | 2.24E+03 | 2.27E+03 | 2.29E+03 | 2.23E+03 | 2.36E+03 |
| | Max | 2.23E+03 | 2.35E+03 | 2.27E+03 | 2.24E+03 | 2.45E+03 | 2.59E+03 | 2.24E+03 | 2.67E+03 |
| | Std | 5.39E+00 | 2.29E+01 | 1.10E+01 | 3.90E+00 | 6.00E+01 | 2.23E+03 | 3.54E+00 | 1.16E+02 |
| F9 | Min | 2.53E+03 | 2.53E+03 | 2.56E+03 | 2.56E+03 | 2.65E+03 | 2.59E+03 | 2.53E+03 | 2.63E+03 |
| | Mean | 2.55E+03 | 2.54E+03 | 2.64E+03 | 2.59E+03 | 2.75E+03 | 2.67E+03 | 2.60E+03 | 2.78E+03 |
| | Max | 2.59E+03 | 2.59E+03 | 2.70E+03 | 2.63E+03 | 2.95E+03 | 2.74E+03 | 2.68E+03 | 2.99E+03 |
| | Std | 1.95E+01 | 2.51E+01 | 4.89E+01 | 2.35E+01 | 1.04E+02 | 2.59E+03 | 4.99E+01 | 1.09E+02 |
| F10 | Min | 2.50E+03 | 2.50E+03 | 2.50E+03 | 2.50E+03 | 2.52E+03 | 2.50E+03 | 2.50E+03 | 2.50E+03 |
| | Mean | 2.55E+03 | 2.66E+03 | 2.65E+03 | 2.50E+03 | 2.66E+03 | 2.56E+03 | 2.59E+03 | 2.54E+03 |

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|-----|------|----------|----------|----------|----------|----------|----------|----------|
| F11 | Max | 2.64E+03 | 3.17E+03 | 3.69E+03 | 2.50E+03 | 2.96E+03 | 2.78E+03 | 2.65E+03 |
| | Std | 6.51E+01 | 2.64E+02 | 3.71E+02 | 8.44E-01 | 1.27E+02 | 2.50E+03 | 6.27E+01 |
| | Min | 2.61E+03 | 2.60E+03 | 2.72E+03 | 2.77E+03 | 2.90E+03 | 2.68E+03 | 2.73E+03 |
| | Mean | 2.71E+03 | 2.96E+03 | 2.90E+03 | 2.79E+03 | 3.29E+03 | 3.04E+03 | 3.00E+03 |
| F12 | Max | 2.92E+03 | 3.41E+03 | 3.20E+03 | 2.82E+03 | 3.96E+03 | 3.94E+03 | 3.33E+03 |
| | Std | 1.29E+02 | 2.77E+02 | 1.76E+02 | 1.43E+01 | 4.15E+02 | 2.68E+03 | 2.37E+02 |
| | Min | 3.35E+02 | 5.22E+02 | 6.44E+03 | 7.74E+02 | 8.49E+03 | 6.16E+03 | 5.08E+02 |
| | Mean | 1.22E+03 | 1.22E+04 | 2.44E+04 | 2.47E+03 | 1.37E+04 | 8.76E+03 | 4.70E+03 |
| F12 | Max | 2.95E+03 | 7.43E+04 | 3.84E+04 | 5.74E+03 | 2.75E+04 | 1.05E+04 | 9.10E+03 |
| | Std | 7.64E+02 | 2.23E+04 | 1.06E+04 | 1.39E+03 | 6.70E+03 | 6.16E+03 | 3.06E+03 |
| | | | | | | | | 2.16E+03 |

Table 6. The comparison results 12 functions using CEC 2022 and Dim=20

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|----|------|----------|----------|----------|----------|----------|----------|----------|
| F1 | Min | 8.64E+03 | 2.55E+04 | 2.59E+04 | 1.03E+04 | 2.79E+04 | 3.29E+04 | 7.23E+03 |
| | Mean | 1.32E+04 | 6.56E+04 | 3.39E+04 | 1.91E+04 | 5.32E+04 | 4.80E+04 | 1.55E+04 |
| | Max | 1.73E+04 | 1.50E+05 | 5.22E+04 | 3.02E+04 | 8.00E+04 | 6.27E+04 | 2.32E+04 |
| | Std | 2.65E+03 | 3.59E+04 | 7.91E+03 | 5.60E+03 | 1.75E+04 | 3.29E+04 | 4.23E+03 |
| F2 | Min | 5.06E+02 | 4.31E+02 | 5.18E+02 | 6.27E+02 | 1.25E+03 | 6.81E+02 | 5.00E+02 |
| | Mean | 6.07E+02 | 5.04E+02 | 6.32E+02 | 7.95E+02 | 2.75E+03 | 1.19E+03 | 6.33E+02 |
| | Max | 6.85E+02 | 7.83E+02 | 7.87E+02 | 1.19E+03 | 4.50E+03 | 2.01E+03 | 8.33E+02 |
| | Std | 4.21E+01 | 7.64E+01 | 6.54E+01 | 1.10E+02 | 7.40E+02 | 6.81E+02 | 9.06E+01 |
| F3 | Min | 6.16E+02 | 6.07E+02 | 6.54E+02 | 6.35E+02 | 6.52E+02 | 6.44E+02 | 6.13E+02 |
| | Mean | 6.36E+02 | 6.21E+02 | 6.75E+02 | 6.52E+02 | 6.79E+02 | 6.67E+02 | 6.26E+02 |
| | Max | 6.51E+02 | 6.32E+02 | 7.01E+02 | 6.66E+02 | 6.91E+02 | 6.82E+02 | 6.45E+02 |
| | Std | 1.28E+01 | 7.73E+00 | 1.53E+01 | 1.01E+01 | 1.19E+01 | 6.44E+02 | 9.62E+00 |
| F4 | Min | 8.59E+02 | 8.66E+02 | 8.88E+02 | 9.16E+02 | 9.44E+02 | 9.10E+02 | 8.60E+02 |
| | Mean | 8.75E+02 | 9.00E+02 | 9.31E+02 | 9.51E+02 | 9.67E+02 | 9.21E+02 | 8.93E+02 |
| | Max | 9.03E+02 | 9.92E+02 | 9.66E+02 | 9.72E+02 | 9.90E+02 | 9.40E+02 | 9.24E+02 |
| | Std | 1.19E+01 | 4.10E+01 | 2.86E+01 | 1.63E+01 | 1.66E+01 | 9.10E+02 | 1.92E+01 |
| F5 | Min | 1.39E+03 | 1.43E+03 | 2.53E+03 | 1.99E+03 | 2.95E+03 | 2.52E+03 | 1.57E+03 |
| | Mean | 1.96E+03 | 3.19E+03 | 3.61E+03 | 2.91E+03 | 3.38E+03 | 2.58E+03 | 2.15E+03 |
| | Max | 2.52E+03 | 7.53E+03 | 5.53E+03 | 4.02E+03 | 4.09E+03 | 2.64E+03 | 2.84E+03 |
| | Std | 3.52E+02 | 1.92E+03 | 8.07E+02 | 7.62E+02 | 3.12E+02 | 2.52E+03 | 3.90E+02 |
| F6 | Min | 2.60E+03 | 7.35E+03 | 5.26E+05 | 4.35E+07 | 9.96E+08 | 1.11E+04 | 1.81E+04 |
| | Mean | 5.03E+03 | 1.22E+07 | 3.73E+06 | 2.28E+08 | 1.92E+09 | 2.27E+08 | 1.61E+07 |
| | Max | 1.07E+04 | 5.30E+07 | 2.21E+07 | 5.33E+08 | 3.34E+09 | 5.95E+08 | 6.11E+07 |
| | Std | 2.40E+03 | 1.96E+07 | 6.52E+06 | 1.59E+08 | 8.08E+08 | 1.11E+04 | 2.06E+07 |
| F7 | Min | 2.04E+03 | 2.04E+03 | 2.10E+03 | 2.12E+03 | 2.11E+03 | 2.19E+03 | 2.05E+03 |
| | Mean | 2.08E+03 | 2.23E+03 | 2.18E+03 | 2.14E+03 | 2.20E+03 | 2.31E+03 | 2.11E+03 |
| | Max | 2.15E+03 | 2.49E+03 | 2.28E+03 | 2.24E+03 | 2.29E+03 | 2.46E+03 | 2.20E+03 |
| | Std | 3.67E+01 | 1.60E+02 | 6.08E+01 | 3.84E+01 | 6.70E+01 | 2.19E+03 | 5.11E+01 |
| F8 | Min | 2.23E+03 | 2.23E+03 | 2.23E+03 | 2.25E+03 | 2.26E+03 | 2.26E+03 | 2.23E+03 |
| | Mean | 2.27E+03 | 2.29E+03 | 2.29E+03 | 2.29E+03 | 2.81E+03 | 2.52E+03 | 2.27E+03 |
| | Max | 2.45E+03 | 2.40E+03 | 2.50E+03 | 2.42E+03 | 6.31E+03 | 3.00E+03 | 2.36E+03 |
| | Std | 6.40E+01 | 6.19E+01 | 7.48E+01 | 4.61E+01 | 9.32E+02 | 2.26E+03 | 5.14E+01 |
| F9 | Min | 2.48E+03 | 2.48E+03 | 2.53E+03 | 2.59E+03 | 2.87E+03 | 2.59E+03 | 2.53E+03 |
| | Mean | 2.49E+03 | 2.50E+03 | 2.58E+03 | 2.65E+03 | 3.22E+03 | 2.72E+03 | 2.61E+03 |
| | Max | 2.50E+03 | 2.55E+03 | 2.61E+03 | 2.75E+03 | 3.89E+03 | 2.85E+03 | 2.68E+03 |
| | Std | 6.13E+00 | 2.93E+01 | 3.03E+01 | 5.37E+01 | 3.59E+02 | 2.59E+03 | 4.28E+01 |

| F | SBOA | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|-----|------|----------|----------|----------|----------|----------|----------|----------|
| F10 | Min | 2.50E+03 | 2.50E+03 | 2.50E+03 | 2.52E+03 | 2.65E+03 | 2.77E+03 | 2.52E+03 |
| | Mean | 2.66E+03 | 4.65E+03 | 5.16E+03 | 3.65E+03 | 5.75E+03 | 5.28E+03 | 4.26E+03 |
| | Max | 4.66E+03 | 6.05E+03 | 6.97E+03 | 6.96E+03 | 7.38E+03 | 6.39E+03 | 7.09E+03 |
| | Std | 4.35E+02 | 1.09E+03 | 1.11E+03 | 1.73E+03 | 1.53E+03 | 2.77E+03 | 1.71E+03 |
| F11 | Min | 3.32E+03 | 2.91E+03 | 3.99E+03 | 3.83E+03 | 7.84E+03 | 5.07E+03 | 4.02E+03 |
| | Mean | 3.45E+03 | 4.66E+03 | 4.61E+03 | 5.08E+03 | 8.49E+03 | 6.72E+03 | 4.27E+03 |
| | Max | 3.65E+03 | 8.15E+03 | 5.83E+03 | 5.87E+03 | 9.11E+03 | 8.41E+03 | 4.59E+03 |
| | Std | 1.73E+02 | 3.02E+03 | 1.06E+03 | 1.09E+03 | 6.33E+02 | 5.07E+03 | 2.88E+02 |
| F12 | Min | 3.15E+03 | 3.17E+03 | 3.24E+03 | 3.26E+03 | 3.35E+03 | 3.43E+03 | 3.16E+03 |
| | Mean | 3.20E+03 | 3.21E+03 | 3.31E+03 | 3.32E+03 | 3.69E+03 | 3.98E+03 | 3.22E+03 |
| | Max | 3.25E+03 | 3.28E+03 | 3.50E+03 | 3.38E+03 | 4.06E+03 | 4.49E+03 | 3.34E+03 |
| | Std | 3.55E+01 | 4.26E+01 | 8.42E+01 | 4.48E+01 | 2.47E+02 | 3.43E+03 | 5.04E+01 |

Table 7,
 Table 8 show two the wilcoxon rank sum test results for SBOA against other algorithms CEC 2022 Dim = 10 and Dim=20. From these tables, the

phenomenon that most values less than 0.05 is confirmed that SBOA is the best algorithm in all algorithms.

Table 7. Wilcoxon rank sum test results for SBOA against other algorithms CEC2022 Dim = 10

| Function | DE | SCA | WOA | LSO | SSA | GJO | BOA |
|----------|----------|----------|----------|----------|----------|----------|----------|
| F1 | 3.76E-02 | 1.83E-04 | 1.73E-02 | 1.83E-04 | 1.83E-04 | 4.59E-03 | 2.46E-04 |
| F3 | 8.77E-02 | 4.08E-05 | 7.12E-09 | 3.02E-11 | 1.86E-06 | 1.25E-05 | 3.02E-11 |
| F4 | 1.17E-04 | 3.02E-11 | 3.34E-11 | 3.02E-11 | 3.34E-11 | 3.56E-04 | 3.02E-11 |
| F5 | 1.47E-07 | 2.15E-10 | 3.34E-11 | 3.69E-11 | 1.56E-08 | 2.68E-04 | 3.02E-11 |
| F6 | 2.77E-05 | 4.08E-11 | 3.20E-09 | 3.34E-11 | 3.02E-11 | 3.56E-04 | 3.02E-11 |
| F7 | 3.82E-09 | 3.82E-10 | 3.02E-11 | 3.02E-11 | 5.87E-04 | 3.34E-11 | 3.02E-11 |
| F8 | 3.15E-02 | 2.76E-03 | 1.65E-04 | 4.11E-05 | 4.11E-05 | 1.85E-03 | 4.11E-05 |
| F9 | 2.15E-02 | 1.01E-08 | 3.82E-10 | 8.89E-10 | 1.29E-09 | 2.89E-03 | 3.34E-11 |
| F10 | 4.35E-02 | 5.83E-04 | 3.61E-03 | 1.83E-04 | 2.46E-04 | 2.11E-02 | 1.83E-04 |
| F11 | 6.40E-02 | 1.40E-02 | 6.40E-02 | 3.30E-04 | 1.40E-02 | 7.28E-03 | 3.30E-04 |
| F12 | 3.45E-01 | 7.69E-04 | 2.41E-01 | 4.40E-04 | 1.83E-04 | 4.73E-01 | 2.46E-04 |

Table 8. Wilcoxon rank sum test results for SBOA against other algorithms CEC2022 Dim = 20

| Function | DE | POA | WOA | LSO | SSA | GJO | GWO |
|----------|----------|----------|----------|----------|----------|----------|----------|
| F1 | 1.83E-04 | 1.83E-04 | 5.80E-03 | 1.83E-04 | 1.83E-04 | 5.39E-02 | 1.83E-04 |
| F3 | 2.20E-07 | 1.22E-01 | 8.99E-11 | 3.02E-11 | 3.34E-11 | 4.46E-01 | 3.02E-11 |
| F4 | 1.40E-02 | 1.83E-04 | 7.28E-03 | 1.83E-04 | 5.83E-04 | 1.04E-01 | 1.83E-04 |
| F5 | 1.21E-01 | 2.46E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 3.12E-02 | 1.83E-04 |
| F6 | 1.86E-01 | 1.83E-04 | 3.61E-03 | 1.83E-04 | 3.30E-04 | 3.45E-01 | 3.30E-04 |
| F7 | 2.46E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 |
| F8 | 3.76E-02 | 7.69E-04 | 5.80E-03 | 7.69E-04 | 1.83E-04 | 1.04E-01 | 1.83E-04 |
| F9 | 6.79E-02 | 2.56E-02 | 3.97E-03 | 5.23E-07 | 3.07E-06 | 4.73E-01 | 9.17E-08 |
| F10 | 5.71E-01 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 | 1.83E-04 |
| F11 | 5.46E-09 | 4.57E-09 | 3.59E-05 | 1.96E-10 | 5.49E-11 | 9.53E-07 | 1.87E-05 |
| F12 | 8.35E-03 | 4.09E-01 | 1.79E-04 | 6.80E-08 | 1.23E-07 | 4.99E-02 | 6.80E-08 |

Engineering Problems

Engineering design optimization problems involve many inequalities constraints, are used to search maximum or minimum¹⁹. Their essences are known as mathematical problems, so many algorithms can be used to get the best value. To prove efficiency, SBOA is used solving 4 constrained problems in this subsection. Welded Beam Design²⁰, Pressure Vessel Design²¹, Gear Train Design²², and Three Bar Truss Design²³.

Pressure vessel design problem

Pressure vessel design problem has 4 design variables(x_1-x_4), the goal of this problem finds minimum. The equations as follow:

The objective function:

Table 9, Error! Reference source not found..

Table 9 shows the best solution $x = [0.9559055314 \ 0.4725024408 \ 49.52835701 \ 116.4764305]$ and where $f(x) = 5920.777474$. From **Error! Reference source not found.** and Figure 1 the SBOA outperform another algorithm.

Welded beam design problem

Welded beam design problem has 4 decision variables(x_1-x_4), the goal is to find the minimum because of cost savings. The equations of Welded beam design problem are shown below:

The objective function:

$$f(\vec{x}) = 1.10471x_1^2x_2 + 0.04811x_3x_4(14.0 + x_2)$$

$$g_1(\vec{x}) = \tau(\vec{x}) - 13,600 \leq 0$$

$$g_2(\vec{x}) = \sigma(\vec{x}) - 30,000 \leq 0$$

$$g_3(\vec{x}) = x_1 - x_4 \leq 0$$

$$g_4(\vec{x}) = 0.10471x_1^2 + 0.04811x_3x_4(14.0 + x_2) - 5.0 \leq 0$$

$$g_5(\vec{x}) = 0.125 - x_1 \leq 0$$

$$g_6(\vec{x}) = \sigma(\vec{x}) - 0.250$$

$$g_7(\vec{x}) = 6,000 - p_c(\vec{x}) \leq$$

$$f(\vec{x}) = 0.6224x_1x_3x_4 + 1.7781x_2x_3^2 + 3.1661x_1^2x_4 + 19.84x_1^2x_3$$

Subject to:

$$g_1(\vec{x}) = -x_1 + 0.0193x_3 \leq 0$$

$$g_2(\vec{x}) = -x_2 + 0.00954x_3 \leq 0$$

$$g_3(\vec{x}) = -\pi x_3^2 x_4^2 - \frac{4}{3}\pi x_3^3 + 1,296,000 \leq 0$$

$$g_4(\vec{x}) = x_4 - 240 \leq 0$$

$$\text{with } 1 \times 0.0625 \leq x_1, x_2 \leq 99 \times 0.0625$$

$$10.0 \leq x_3, x_4 \leq 200.0$$

Results of SBOA and other algorithms are given in

Subject to:

$$\tau(\vec{x}) = \sqrt{(\tau')^2 + (2\tau'\tau'')\frac{x^2}{2R} + (\tau'')^2}$$

$$\tau' = \frac{6,000}{\sqrt{2}x_1x_2}, \tau'' = \frac{MR}{J}$$

$$M = 6,000 \left(14 + \frac{x_2}{2} \right)$$

$$R = \sqrt{\frac{x_2^2}{4} + \left(\frac{x_1 + x_3}{2} \right)^2}$$

$$J = 2 \left\{ x_1x_2\sqrt{2} \left[\frac{x_2^2}{12} + \left(\frac{x_1 + x_3}{2} \right)^2 \right] \right\}$$

$$\sigma(\vec{x}) = \frac{504,000}{x_4x_3^2}, \delta(\vec{x}) = \frac{65,856,000}{(30 \times 10^6)x_4x_3^2}$$

$$P_c(\vec{x}) = \frac{4.013(30 \times 10^6)\sqrt{\frac{x_3^2x_4}{36}}}{196} \left(1 - \frac{x_3\sqrt{\frac{30 \times 10^6}{4(12 \times 10^6)}}}{28} \right)$$

$$\text{with } 0.1 \leq x_1, x_4 \leq 2.0 \text{ and } 0.1 \leq x_2, x_3 \leq 10.0$$

Results of SBOA and other algorithms are given in **Error! Reference source not found.**, **Error! Reference source not found.**, and **Error!**

Reference source not found.. Error! Reference source not found. shows the best solution $x=[0.2057296398, 3.470488666, 9.03662391, 0.2057296398]$ and where $f(x)=1.724852309$. From **Error! Reference source not found.** and **Error! Reference source not found.**, the SBOA algorithm is better than other algorithms, and convergence rate is best.

Gear train design problem

This problem has 2 design variables(x_1-x_4), the goal is to find minimum gear ratios. The equation of the problem is shown below:

The objective function:

$$f(\vec{x}) = \left(\frac{1}{6.931} - \frac{x_2 x_3}{x_1 x_4} \right)^2$$

$$12 \leq x_1, x_2, x_3, x_4 \leq 60$$

Results of SBOA and other algorithms are given in **Error! Reference source not found.. Error! Reference source not found.**, and **Error! Reference source not found.. Error! Reference source not found.** shows the best solution $x=[44.51174489, 14.4911759, 22.15518804, 45.55514392]$ and where $f(x)=0$. From **Error! Reference source not found.** and **Error!**

Reference source not found.. the SBOA outperforms another algorithm.

Three Bar Truss Design problem

This problem has 2 design variables(x_1-x_2), the goal is to find minimum volume. The equation of the problem is shown below:

The objective function:

$$f(\vec{x}) = (\sqrt{2}x_1 + x_2) * 100$$

$$g_1(\vec{x}) = 2 \frac{x_2}{\sqrt{2}x_1^2 + 2x_1x_2} - 2 \leq 0$$

$$g_2(\vec{x}) = 2 \frac{\sqrt{2}x_1 + x_2}{\sqrt{2}x_1^2 + 2x_1x_2} - 2 \leq 0$$

$$g_3(\vec{x}) = \frac{2}{\sqrt{2}x_1^2 + 2x_1x_2} \leq 0$$

with $0 \leq x_1, x_2 \leq 1$

Results of SBOA and other algorithms are given in **Error! Reference source not found.. Error! Reference source not found..**, and **Error! Reference source not found.. Error! Reference source not found.. Error! Reference source not found.** shows the best solution $x=[0.7886781057, 0.4082398906, 10.06165022]$ and where $f(x)=263.8958437$. From **Error! Reference source not found.. Error! Reference source not found..**, the SBOA outperform other algorithm.

Table 9. Comparison of optimum results for Pressure Vessel Design

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|------|----------|-----------|-----------|-----------|-----------|-----------|----------|-----------|
| X1 | 0.955905 | 0.9630441 | 0.8342906 | 1.0327819 | 0.9559055 | 0.7781686 | 3.832522 | 0.8837330 |
| | 5314 | 167 | 945 | 36 | 314 | 414 | 915 | 516 |
| X2 | 0.472502 | 0.4760880 | 0.4124245 | 0.5041908 | 0.4725024 | 0.3846491 | 9.866387 | 0.5640434 |
| | 4408 | 365 | 68 | 999 | 408 | 626 | 089 | 348 |
| X3 | 49.52835 | 49.894289 | 43.227437 | 51.256512 | 49.528357 | 40.319618 | 56.23997 | 44.804428 |
| | 701 | 48 | 64 | 42 | 01 | 72 | 968 | 72 |
| X4 | 116.4764 | 103.06116 | 166.13378 | 109.25068 | 116.47643 | 200.00000 | 59.23882 | 156.39804 |
| | 305 | 95 | 68 | 45 | 05 | 000 | 293 | 03 |
| cost | 5920.777 | 5885.8260 | 6267.9908 | 6232.1187 | 6639.7536 | 82027.166 | 6089.760 | 6514.5341 |
| | 474 | 56 | 16 | 71 | 12 | 52 | 092 | 63 |

Table 10. Statistical results for Pressure Vessel Design

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Best | 5920.7774 | 5885.8260 | 6267.9908 | 6232.1187 | 6639.7536 | 82027.166 | 6089.7600 | 6514.5341 |
| | 74 | 56 | 16 | 71 | 12 | 52 | 92 | 63 |
| Mea | 6330.7994 | 5995.8313 | 6792.7834 | 6462.7782 | 5885.3327 | 82524.583 | 6171.6834 | 6954.5041 |
| n | 18 | 66 | 66 | 94 | 74 | 58 | 26 | 13 |
| Wors | 6740.8213 | 6105.8366 | 7317.5761 | 6693.4378 | 5885.3327 | 83022.000 | 6253.6067 | 7394.4740 |
| t | 61 | 77 | 16 | 16 | 74 | 64 | 61 | 64 |
| Std | 579.85859 | 155.57100 | 742.16888 | 326.20182 | 0 | 703.45395 | 115.85709 | 622.21147 |



36 18 31 49 25 07 1

Table 11. Comparison of optimum results for Welded beam design problem

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|------|------------------|------------------|------------------|------------------|--------------------------|--------------------------|------------------|------------------|
| X1 | 0.2057296 398 | 0.22105386 47 | 0.20573118 78 | 0.20505394 42 | 0.15642297 38 | 0.20572963 98 | 0.51631647 59 | 0.20598696 26 |
| X2 | 3.4704886 66 | 3.28940617 4 | 3.47047259 6 | 3.69562116 6 | 5.25920935 6 | 3.47048866 6 | 2.33197453 2 | 3.74658012 4 |
| X3 | 9.0366239 1 | 8.72295750 7 | 9.03657923 2 | 8.68578509 5 | 9.08891081 9.03662391 | 9.03662391 4.66046847 | 4.66046847 2 | 8.98679980 3 |
| X4 | 0.2057296 398 | 0.22121587 56 | 0.20573167 53 | 0.22870067 03 | 0.20632132 67 | 0.20572963 98 | 0.81954580 76 | 0.21463633 08 |
| cost | 1.7248523 09 | 1.74215940 2 | 1.72485306 4 | 1.82694584 7 | 1.83489995 3 | 1.72485230 9 | 3.29808700 9 | 1.81139074 9 |

Table 12. Statistical results for Welded beam design problem

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|------|---------------------|-------------------|---------------------|-------------------|-------------------|---------------------|------------------|--------------------|
| Best | 1.72485230 9 | 1.742159402 4 | 1.72485306 | 1.826945847 | 1.834899953 | 1.72485230 9 | 3.29808700 9 | 1.811390749 731 |
| Mea | 1.72485230 | 1.780303494 | 1.72486029 | 1.855640797 | 1.878859267 | 1.72485230 | 3.62274751 | 1.822373861 |
| n | 9 | | 7 | | | 9 | 3 | 9 |
| Wors | 1.72485230 t 9 | 1.818447586 9 | 1.72486752 | 1.884335747 | 1.922818582 | 1.72485230 9 | 3.94740801 7 | 1.833356973 3 |
| Std | 3.14018491 7e-16 | 0.053943891 76 | 1.02279592 5e-05 | 0.040580787 67 | 0.062167858 47 | 9.31724266 8e-12 | 0.45913928 74 | 0.015532465 57 |

Table 13. Comparison of optimum results for Three Bar Truss Design

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|-------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
| x1 | 0.788678105 7 | 0.788591298 1 | 0.789556350 4 | 0.789981212 7 | 0.788588539 4 | 0.788675134 2 | 0.774968466 6 | 0.783291370 5 |
| x2 | 0.408239890 6 | 0.408498459 6 | 0.433720857 1 | 0.405655991 6 | 0.408500096 | 0.408248291 6 | 0.453659454 4 | 0.424256997 5 |
| cos t | 263.8958437 t | 263.8969781 | 264.905777 | 263.9872784 | 263.8964062 | 263.8958434 | 264.2747612 | 263.9365898 |

Table 14. Statistical results for Three Bar Truss Design

| | SBOA | SSA | BOA | WOA | HHO | DE | LSO | SCA |
|------|---------------------|---------------------|--------------------------|-------------------|---------------------|-----------------|------------------|-------------------|
| Best | 263.895843 7 | 263.8969781 7 | 264.90577 7 | 263.9872784 | 263.8964062 | 263.89584 34 | 264.274761 2 | 263.9365898 |
| Mea | 263.895843 n 7 | 263.8971478 55 | 266.69234 264.0060282 | 263.8965311 | | 263.89584 34 | 264.560128 6 | 263.9739556 |
| Wor | 263.895843 st 8 | 263.8973174 4 | 268.47891 264.024778 | 263.896656 34 | | 263.89584 34 | 264.845496 1 | 264.0113215 |
| Std | 1.37862016 1e-07 | 0.0002399571 797 | 2.5265894 22 | 0.026516225 75 | 0.0001766404 548 | 0 | 0.40357053 69 | 0.052843334 57 |

Table 15. Comparison of optimum results for Gear train design

| | SBOA | SSA | GWO | WOA | HHO | POA | LSO | SCA |
|----|-----------------|-----------------|------------------|------------------|-----------------|-----------------|-----------------|-------------|
| x1 | 44.5117 4489 | 53.355 76307 | 53.0497738 7 | 50.848895 91 | 46.85152 488 | 32.725243 63 | 41.8728313 8 | 60 |
| x2 | 14.4911 759 | 28.381 001 | 19.3136642 22 | 18.281417 574 | 28.23560 65 | 14.049780 1 | 17.5277852 | 32.99962809 |
| x3 | 22.1551 8804 | 16.594 66426 | 20.1066208 7 | 20.580351 55 | 14.20541 526 | 12.409361 58 | 15.7365467 8 | 17.43096945 |



| | | | | | | | | |
|----|---------|--------|------------|-----------|-----------|-----------|------------|-----------------|
| x | 45.5551 | 55.303 | 35.2759503 | 46.507649 | 59.18020 | 39.562359 | 45.6736660 | 60 |
| 4 | 4392 | 88372 | 9 | 09 | 488 | 89 | 1 | |
| c | 0.00000 | 5.6160 | 0.00027634 | 0.0000000 | 0.0000000 | 3.7748226 | 7.13756210 | 1.604807594e-12 |
| o | 00000 | 11718e | 58932 | 000 | 0000 | 91e-32 | 4e-11 | |
| st | | | -31 | | | | | |

Table 16. Statistical results for Gear train design

| | SBOA | SSA | GWO | WOA | HHO | POA | LSO | SCA |
|-------|-----------|------------|------------|-----------|-----------|------------|------------|-----------|
| Best | 0.0000000 | 5.61601171 | 0.00027634 | 0.0000000 | 0.0000000 | 3.77482269 | 7.13756210 | 1.6048075 |
| | 000 | 8e-31 | 58932 | 000 | 000 | 1e-32 | 4e-11 | 94e-12 |
| Mean | 0.0000000 | 9.08754852 | 0.00353192 | 0.0000000 | 0.0000000 | 1.05540961 | 3.89309950 | 2.3222941 |
| | 000 | 2e-15 | 6614 | 000 | 000 | e-31 | 7e-09 | 68e-10 |
| Worst | 0.0000000 | 1.81750970 | 0.00678750 | 0.0000000 | 0.0000000 | 1.73333695 | 7.71482339 | 4.6285402 |
| | 000 | 4e-14 | 7335 | 000 | 000 | e-31 | 3e-09 | 59e-10 |
| Std | 0.0000000 | 1.28517343 | 0.00460408 | 0.0000000 | 0.0000000 | 9.58734039 | 5.40473375 | 3.2615245 |
| | 000 | 7e-14 | 6409 | 000 | 000 | 1e-32 | 1e-09 | 01e-10 |

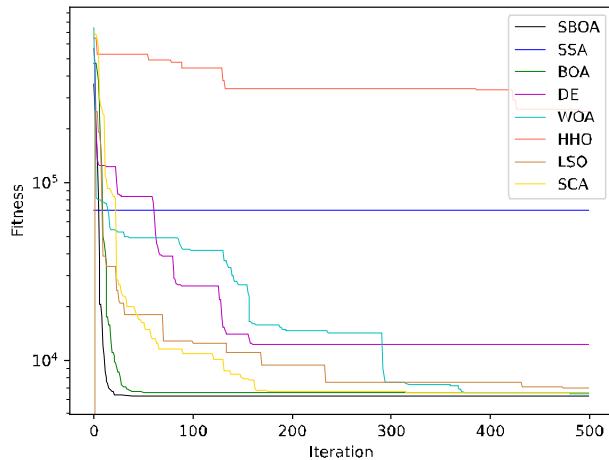


Figure 1. Pressure vessel design

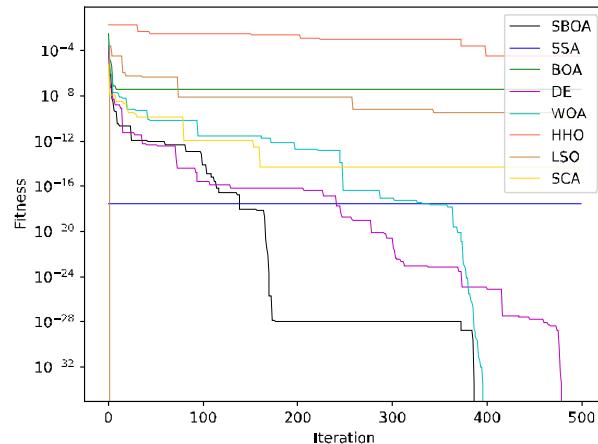


Figure 5. Gear train design problem

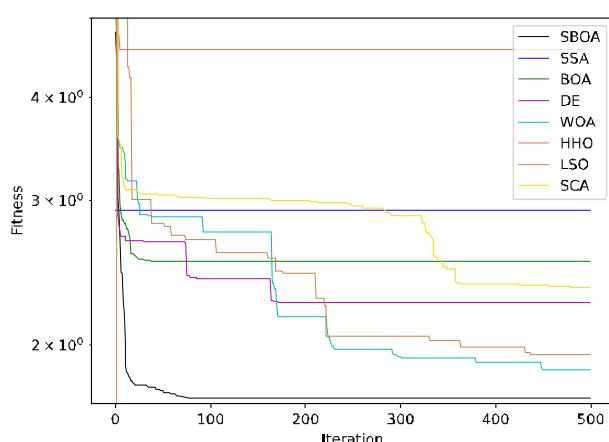


Figure 2. Welded beam design problem

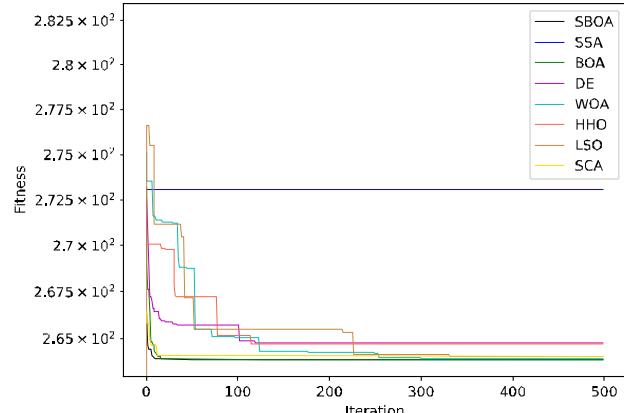


Figure 6. Three bar truss design

Conclusions

SBOA is proposed in this study and used 3 different benchmark functions to test performance and other well-known algorithms as DE, SSA, SCA, BOA,

WOA, HHO, LSO, GJO. The results of these tables and figures show that SBOA is a feasible and



simple algorithm, it is better than the above

comparative algorithms.

Acknowledgment

The writer would like to express gratitude to Wenzhou Association for Science and Technology

(grant No. jcjc118), for their assistance with this project.

Authors' Declaration

- Conflicts of Interest: None.
- We hereby confirm that all the Figures and Tables in the manuscript are ours. Furthermore, any Figures and images, that are not ours, have been included with the necessary permission for

re-publication, which is attached to the manuscript.

- Ethical Clearance: The project was approved by the local ethical committee in Universiti Teknologi Malaysia

Authors' Contribution Statement

D.Q wrote the manuscript with design and analysis, A.J edited the manuscript with revisions, C.W.H and A.M.Z. gave the idea of research and the tips of

work. Y.H collected the literature. All authors read and approved the final manuscript.

References

1. Almufti SM, Shaban AA, Ali ZA, Ali RI, Fuente JAD. Overview of Metaheuristic Algorithms. PGJSRT. 2023;2(2):10-32. <https://doi.org/10.58429/pgjsrt.v2n2a144>.
2. Jassim OA, Abed MJ, Saeid ZH. Indoor/Outdoor Deep Learning Based Image Classification for Object Recognition Applications. Baghdad Sci J. 2023;20(6(Suppl.)):2540. <https://doi.org/10.21123/bsj.2023.8177>.
3. Gen M, Lin L. Genetic algorithms and their applications. Springer handbook of engineering statistics: Springer. 2023;p. 635-74.
4. Song Y, Cai X, Zhou X, Zhang B, Chen H, Li Y, et al. Dynamic hybrid mechanism-based differential evolution algorithm and its application. Expert Syst Appl. 2023;213:118834. https://doi.org/10.1007/978-1-4471-7503-2_33.
5. Khurma RA, Albashish D, Braik M, Alzaqebah A, Qasem A, Adwan O. An augmented Snake Optimizer for diseases and COVID-19 diagnosis. Biomed Signal Proces. 2023;84:104718. <https://doi.org/10.1016/j.bspc.2023.104718>.
6. Gad AG, Sallam KM, Chakrabortty RK, Ryan MJ, Abohany AA. An improved binary sparrow search algorithm for feature selection in data classification. Neural Computing and Applications. 2022;34(18):15705-52. <https://doi.org/10.1007/s00521-022-07203-7>.
7. Chopra N, Ansari MM. Golden jackal optimization: A novel nature-inspired optimizer for engineering applications. Expert Syst Appl. 2022;198:116924. <https://doi.org/10.1016/j.eswa.2022.116924>.
8. Trojovský P, Dehghani M. Pelican optimization algorithm: A novel nature-inspired algorithm for engineering applications. Sensors-Basel. 2022;22(3):855. <https://doi.org/10.3390/s22030855>.
9. Bacanin N, Zivkovic M, Al-Turjman F, Venkatachalam K, Trojovský P, Strumberger I, et al. Hybridized sine cosine algorithm with convolutional neural networks dropout regularization application. Sci Rep-Uk. 2022;12(1):6302. <https://doi.org/10.1038/s41598-022-09744-2>.
10. Tang C, Sun W, Xue M, Zhang X, Tang H, Wu W. A hybrid whale optimization algorithm with artificial bee colony. Soft Comput. 2022;26(5):2075-97. <https://doi.org/10.1007/s00500-021-06623-2>.
11. Meidani K, Hemmasian A, Mirjalili S, Barati Farimani A. Adaptive grey wolf optimizer. Neural Computing and Applications. 2022;34(10):7711-31. <https://doi.org/10.1007/s00521-021-06885-9>.
12. Khodadadi N, Talatahari S, Dadras Eslamlou A. MOTEQ: a novel multi-objective thermal exchange optimization algorithm for engineering problems. Soft Comput. 2022;26(14):6659-84. <https://doi.org/10.1007/s00500-022-07050-7>.
13. Kommadath R, Maharana D, Sivadurgaprasad C, Kotecha P. Parallel computing strategies for sanitized teaching learning based optimization. J Comput Sci-Neth. 2022;63:101766. <https://doi.org/10.1016/j.jocs.2022.101766>.



14. Das B, Mukherjee V, Das D. Student psychology based optimization algorithm: A new population based optimization algorithm for solving optimization problems. *Adv. Eng. Softw.* . 2020;146:102804. <https://doi.org/10.1016/j.advengsoft.2020.102804>.
15. Dorigo M, Stützle T. *Ant colony optimization: overview and recent advances*: Springer. 2019. https://doi.org/10.1007/978-3-319-91086-4_10.
16. Ait-Saadi A, Meraihi Y, Soukane A, Ramdane-Cherif A, Gabis AB. A novel hybrid chaotic Aquila optimization algorithm with simulated annealing for unmanned aerial vehicles path planning. *Comput. Electr. Eng.* . 2022;104:108461. <https://doi.org/10.1016/j.compeleceng.2022.108461>.
17. Abdulqader AW, Ali SM. Diversity Operators-based Artificial Fish Swarm Algorithm to Solve Flexible Job Shop Scheduling Problem. *Baghdad Sci J.* . 2023;20(5(Suppl.)). <https://dx.doi.org/10.21123/bsj.2023.6810>.
18. Sharma TK. Enhanced butterfly optimization algorithm for reliability optimization problems. *J Ambient Intell Humaniz Comput.* . 2021;12(7):7595-619. <https://doi.org/10.1007/s12652-020-02481-2>.
19. Mazher AN, Waleed J. Retina Based Glowworm Swarm Optimization for Random Cryptographic Key Generation. *Baghdad Sci J.* . 2022;19(1):0179. <https://doi.org/10.21123/bsj.2022.19.1.017920>.
20. Chugh T, Sindhya K, 20. Hakonen J, Miettinen K. A survey on handling computationally expensive multiobjective optimization problems with evolutionary algorithms. *Soft Comput.* . 2019;23:3137-66. <https://doi.org/10.1007/s00500-017-2965-0>.
21. Li X-D, Wang J-S, Hao W-K, Zhang M, Wang M. Chaotic arithmetic optimization algorithm. *Appl. Intell.* . 2022;52(14):16718-57. <https://doi.org/10.1007/s10489-021-03037-3>.
22. Nasr MF, Maalawi KY, Yihia K. Multi-Objective Optimization of Planetary Gear Train Using Genetic Algorithm. *Journal of International Society for Science and Engineering.* . 2022;4(3):74-80. <https://doi.org/10.21608/JISSE.2022.144284.1059>.
23. Tao D, Wei X, Huang H, editors. *Application of Improved Fruit Fly Optimization Algorithm in Three Bar Truss*. International Conference on Intelligent Computing. 2022 Springer. https://doi.org/10.1007/978-3-031-13832-4_64.

SBOA: خوارزمية تحسين إرشادية جديدة

دياو كي¹, آبرى جنيدى², جان وينك هو², ازلاند موهد زين², يانكهاولونك³

¹ كلية الذكاء الاصطناعي، تشجيانغ دونغفانغ بوليتكنيك، ونزو، 32500، الصين.
² كلية الحاسوبات، الجامعة التكنولوجية الماليزية، 81310، سكوداي، جوهور، ماليزيا.
³ جامعة بوسطن، ماساتشوستس، 02215، أمريكا.

الخلاصة

تم تقديم طريقة تحسين إرشادية جديدة تعتمد على الإنسان، تسمى خوارزمية التحسين المستندة إلى السنوكر (SBOA)، في هذه الدراسة. الإلهام لهذه الطريقة مستوحى من سمات نخبة المبيعات - تلك الصفات التي يطمح كل مندوب مبيعات إلى امتلاكها. عادةً ما يسعى مندوبو المبيعات إلى تعزيز مهاراتهم من خلال التعلم الذاتي أو من خلال طلب التوجيه من الآخرين. علاوة على ذلك، فإنهم يشاركون في اتصالات منتظمة مع العملاء للحصول على الموافقة على منتجاتهم أو خدماتهم. بناءً على هذا المفهوم، تهدف SBOA إلى إيجاد الحل الأمثل ضمن مساحة بحث معينة، واجتياز جميع المواضيع للحصول على جميع القيم الممكنة. لتقييم جدوى وفعالية SBOA مقارنة بالخوارزميات الأخرى، أجرينا اختبارات على عشر وظائف ذات هدف واحد من الوظائف المعيارية لعام 2019 للحساب التطوري (CEC)، بالإضافة إلى أربع وعشرين وظيفة ذات هدف واحد من CEC لعام 2022. وظائف مرجعية، بالإضافة إلى أربع مشاكل هندسية. تم استخدام سبع خوارزميات مقارنة: خوارزمية التطور التقاضلي (DE)، خوارزمية بحث العصفور (SSA)، خوارزمية حبيب القمام (SCA)، خوارزمية تحسين الحيتان (WOA)، خوارزمية تحسين الفراشة (BOA)، تحسين سرب الأسد (LSO)، و تحسين ابن آوى الذهبي (GJO). وتمت مقارنة نتائج هذه التجارب المتعددة من حيث الدقة وسرعة منحني التقارب. تشير النتائج إلى أن SBOA هو نهج مباشر وقابل للتطبيق ويتفوق بشكل عام على الخوارزميات المذكورة أعلاه.

الكلمات المفتاحية: طريقة التحسين الإرشادية، الإحتساب التطوري، وظائف موضوعية واحدة، التعلم الذاتي، مساحة البحث.